HELSINKI UNIVERSITY OF TECHNOLOGY

Department of Civil and Environmental Engineering

VINCENT FLOQUET

MODELLING CREEP OF SOFT FINNISH CLAY

Final Project submitted on 17/08/2006

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This project was done in the Laboratory of Soil Mechanics and foundation engineering at the Helsinki University of Technology (HUT).

The aim of this project was to study the simulation of settlement in the long term i.e. to understand the creep behavior of clay. Indeed the secondary consolidation is a major concern when buildings, roads, embankments and other structures are founded on deep clay layers. This settlement causes high costs of maintenance in the life span of a structure.

To proceed tests have been carried out in the laboratory and data of former long duration oedometer tests have been gathered. These data have then been processed and analysed in order to extract the right parameters defining the different clays. Once these parameters obtained simulations with PLAXIS’ “Soft Soil Creep model” and also classical modelling have been performed. The simulated and observed results have then been compared enabling us to start the reflection about the acquisition of the parameters to model the long term behavior. Attempt to improve this data process, to stick more accurately to the actual behavior, have also been carried out.
PREFACE

I would like to thank Professor Olli Ravaska and Lic.Sc (Tech.) Matti Lojander for their guidance and help that they have given me during this final project. I would also like to thank M.Sc. (Tech.) Timo Stapelfeldt and M.Sc. (Tech.) Hassan Md.Mamunul, from the Helsinki University of Technology, for their time and advice that have been very valuable for me during this project.

In addition, I would like to thank the personnel of the Laboratory of Soil Mechanics and Foundation Engineering at The Helsinki University of Technology and everybody else who have supported me in my work and above all have welcome me so warmly at the laboratory.

Espoo, 17 August 2006

Vincent FLOQUET
LIST OF SYMBOLS

**Roman letters**

\[
B = \frac{m}{r_s} = \frac{C_s}{C_c} \\
C = \frac{1}{r_s} \\
C \quad \text{degree Celsius} \\
C_\alpha \quad \text{secondary compression index} \\
C_c \quad \text{compression index} \\
C_\varepsilon \quad \text{compression index (\%)} \\
C_p \quad \text{preconsolidation index} \\
C_r \quad \text{recompression index} \\
C_s \quad \text{recompression index} \\
c_v \quad \text{coefficient of consolidation} \\
\epsilon \quad \text{void ratio} \\
\epsilon_0 \quad \text{initial void ratio} \\
G \quad \text{rigidity modulus} \\
H \quad \text{drainage length} \\
H_0 \quad \text{height of the sample at t=0} \\
H_{EOP} \quad \text{height of the sample at the end of primary consolidation} \\
K_0 \quad \text{coefficient of earth pressure in consolidated state} \\
K_b \quad \text{bulk compressibility modulus} \\
k \quad \text{permeability or coefficient of permeability} \\
k_v \quad \text{vertical permeability} \\
k_h \quad \text{horizontal permeability} \\
M \quad \text{compression modulus, oedometer modulus} \\
m \quad \text{modulus number} \\
p'_c \quad \text{preconsolidation pressure} \\
R \quad \text{time resistance} \]
$r_s$  time resistance number

$r_0$  initial time resistance number

$S$  settlement

$S_f$  final settlement

$Sp$  preconsolidation pressure

$S_p$  primary settlement

$q$  load

$T_v$  time factor

$t$  time

$t_{90}$  time at 90% of the primary consolidation ($=t_v$)

$t'$  effective creep time

$t_c$  time to the end of primary consolidation

$t_{EOP}$  time to the end of primary consolidation

$t_r$  reference time

$t_0$  time when the R-t curve approaches a straight line

$u$  pore water pressure

$u'$  excess pore pressure

$u_{cr}$  pore water pressure due to creep effects

$V$  specific volume

$w$  a force per unit volume

$w_L$  liquid limit

$w_N$  natural water content

**Greek letters**

$\alpha_s$  coefficient of secondary compression

$\alpha_{smax}$  maximum value of the coefficient of secondary compression

$\beta_{as}$  coefficient of change in secondary compression

$\varepsilon$  strain

$\varepsilon_e$  elastic strain

$\varepsilon_{ep}$  elastic plastic strain
<table>
<thead>
<tr>
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<th>Description</th>
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<tr>
<td>( \varepsilon_v )</td>
<td>vertical strain</td>
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<tr>
<td>( \varepsilon^e_v )</td>
<td>elastic strain during primary consolidation</td>
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<tr>
<td>( \varepsilon^{vp}_v )</td>
<td>strain corresponding to ( \sigma'_p )</td>
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<tr>
<td>( \varepsilon^e_z )</td>
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<td>( \varepsilon^{ep}_z )</td>
<td>vertical elastic plastic strain</td>
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<td>( \varepsilon^p_z )</td>
<td>vertical plastic strain</td>
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<td>( \varepsilon^{tp}_z )</td>
<td>vertical time-dependant strain</td>
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<tr>
<td>( \varepsilon_{cr} )</td>
<td>creep strain</td>
</tr>
<tr>
<td>( \varepsilon^{cr}_{ac} )</td>
<td>creep strain after primary consolidation</td>
</tr>
<tr>
<td>( \varepsilon^{cr}_c )</td>
<td>creep strain during primary consolidation</td>
</tr>
<tr>
<td>( \cdot )</td>
<td>( \varepsilon_{\text{ref}} ) reference strain rate</td>
</tr>
<tr>
<td>( \cdot )</td>
<td>( \varepsilon^e_c ) elastic strain rate during primary consolidation</td>
</tr>
<tr>
<td>( \cdot )</td>
<td>( \varepsilon_v ) vertical strain rate ([1/s])</td>
</tr>
<tr>
<td>( \cdot )</td>
<td>( \varepsilon_{cr} ) creep strain rate</td>
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<tr>
<td>( \cdot )</td>
<td>( \varepsilon^e_v ) vertical elastic strain rate</td>
</tr>
<tr>
<td>( \cdot )</td>
<td>( \varepsilon^{vp}_v ) viscoplastic strain rate</td>
</tr>
<tr>
<td>( \Gamma )</td>
<td>value of ( \log \sigma'_p ) at ( \varepsilon_v = 10^0 ) 1/s</td>
</tr>
<tr>
<td>( \gamma_w )</td>
<td>unit weight of water</td>
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<tr>
<td>( \kappa )</td>
<td>elastic stiffness of soil</td>
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<tr>
<td>( \kappa^* )</td>
<td>modified swelling index</td>
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<tr>
<td>( \lambda )</td>
<td>elastic plastic stiffness of soil</td>
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<td>( \lambda^* )</td>
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<tr>
<td>( \mu^* )</td>
<td>modified creep index</td>
</tr>
<tr>
<td>( v_0 )</td>
<td>coefficient of bulk viscosity</td>
</tr>
<tr>
<td>( v_d )</td>
<td>coefficient of deviatoric viscosity</td>
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**LIST OF SYMBOLS**

\( \sigma \)  
> total stress

\( \sigma' \)  
> effective stress

\( \sigma'_c \)  
> preconsolidation pressure

\( \sigma'_{L} \)  
> effective stress where the compression modulus

\( \sigma'_p \)  
> preconsolidation pressure

\( \sigma'_v \)  
> vertical effective stress \( (\sigma_z) \)

\( \dot{\sigma}_v' \)  
> rate of effective stress change

\( \psi \)  
> creep parameter, \( 1/r_s \)

\( \tau_c \)  
> the intercept with the time axis of the straight creep line

---

**Abbreviations**

CRS  
> Constant rate of Strain

CPT  
> cone penetration test

EOP  
> end of primary consolidation

EVP  
> elastic viscoplastic

IL  
> increment loading

LIR  
> load increment ratio

OCR  
> overconsolidation ratio

POP  
> preoverburden pressure
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1 INTRODUCTION

The compressibility behaviour of soft soil has been a major concern over the past 100 year. As a matter of fact when buildings, roads, embankments and other structures are founded on deep clay layers we often note that after a long period of time a large settlements occurs. This settlement called creep, causes high costs of maintenance in the life span of a structure. Therefore, it is of great importance to be able to calculate and forecast this settlement occurring in the long term.

The objective of this final project is to strive to understand this phenomenon in order to prevent such damages. The soil studied is the particular Finnish clays coming from different sampling sites of Helsinki neighbourhoods and Finland.

To proceed, the existing theories about the creep behaviour of soft clays have been reminded in the first part of the study, from Karl Terzaghi’s first study of consolidation to more modern one, giving thus the basics to understand the phenomenon. Then is exposed a general survey about the tests that had been carried for this work. A focus on the oedometer test (and the long duration procedure) has been made. Indeed it’s the most important test that has been carried as most of the data processed come from these tests. Eventually the last part of the study deals with the simulation, either numerical or classical, of Finnish soft clays behavior. The main tool used for this work was the software “PLAXIS”. A comparison has been made between the results extracted from the tests (oedometer tests) and the results obtained with the numerical model “Soft-Soil-Creep model” (time dependent behaviour). To carry this analysis, a study of the parameters stepping in the simulation has been made focusing on the way to extract properly these parameters from the tests. An analysis of the results’ coherence has led to a notice concerning the validation of numerical computed forecast. Classical simulation has then been carried out to model what couldn’t have been regarded with PLAXIS.
2  THEORIES AND MODELS OF THE CONSOLIDATION PROCESS

2.1  The classical consolidation theory

The classical theory of consolidation was developed by Terzaghi (1923) and first published in 1923. Today, this theory is still the foundation of one dimensional consolidation theory. The theory is based on the assumption that there is a unique relationship between effective stress and strain independent of time. Furthermore, Terzaghi assumes that the modulus as well as the permeability is constant with time /Claesson. 2003/.

The assumption that the relationship between stress and strain, or void ratio, is independent of time is a rough simplification used for high plastic clays since those clays show a large amount of time dependent strains. This can be established by laboratory tests, e.g. incremental loading tests.

Terzaghi’s equation for one dimensional consolidation can be expressed as:

\[
\frac{\partial u}{\partial t} = M \frac{\partial}{\partial z} \left( k \frac{\partial u}{\partial z} \right)
\]

(2.1)

or

\[
\frac{\partial u}{\partial t} = c_v \frac{\partial^2 u}{\partial z^2}
\]

(2.2)

if k does not vary with depth,

Where the coefficient of consolidation is defined as:

\[
c_v = \frac{k M}{\gamma_w}
\]

(2.3)

Where k = permeability [m/s]
M = compression modulus [kPa]
\(\gamma_w = \text{unit weight of water [kN/m}^3]\)
The hydraulic conductivity, \( k \), is in the geotechnical field referred to as permeability or coefficient of permeability.

Equation (2.2) is valid under the following conditions:

- The soil is saturated and homogeneous.
- The flow of pore water flow and the strain are one-dimensional.
- Darcy’s law is valid
- The change in pore water pressure is equal to change in effective stress.
- The pore water and soil particles are incompressible
- The strain is only dependent on the effective stress

In 1925 Terzaghi introduced the first oedometer device and suggested a test procedure where a specimen is loaded step-wise, each load step doubling the previous value, until the excess pore pressure has dissipated. For clays, duration of 24H is quite common. This procedure is still widely used, and is commonly referred to as an incremental load oedometer test.

In 1936 Terzaghi proposed a model for calculating the degree of consolidation

Figure (2.1)

The degree of consolidation is determined by calculating the time factor \( T_v \):

\[
T_v = \frac{c_v}{H^2} t
\]  

(2.4)

Where \( c_v \) = coefficient of consolidation [m\(^2\)/s]

\( H \) = drainage length [m]

\( T \) = time [s]
Figure 2.1 Relationship between time factor and degree of consolidation. The three curves correspond to three different cases of excess pore pressure and drainage conditions.

Casagrande (1936) proposed an oedometer test procedure for determining the end of primary consolidation, EOP, of each load increment, i.e. when the excess pore pressure has completely dissipated.

Figure 2.2 Casagrande method of determining EOP, 100% of primary consolidation.

It assumes that time-strain curve is plotted in a semilogarithmic diagram: The EOP is defined as the point of intersection between the two tangents of the curve as shown in Figure 2.2.
Another commonly used method of determining the EOP was suggested by Taylor (1948). In this method the strain is plotted versus the square root of time.

### 2.2 Early models for consolidation including creep effects

Originally, consolidation settlements were calculated according to Terzaghi’s theory and possibly creep settlements starting after the full excess pore pressure dissipation has occurred, e.g. Buisman (1936). Taylor and Merchant (1940) formulated the first theory where creep effects were at least partly involved in the process of dissipation of excess pore pressure. Two years later, in 1942, Taylor developed a first model of a generation variation of void ratio, $e$, versus effective stress, $\sigma'$, and time, $t$. The model was applicable for oedometer tests.

When the consolidation models have been presented in the literature, the consolidation process has almost always been divided into primary and secondary consolidation. The basics assumption is that the primary consolidation occurs during an increase of the effective stress and a simultaneous decrease of the excess pore pressure and volume. The process of secondary consolidation is defined as a decrease in volume under constant effective stress. Over a long period of time creep strains were separated from the primary consolidation. In 1957, Suklje presented a model, described below, where creep strains also was assumed to occur during primary consolidation. This is the dominating concept for models presented over the 20-30 years.

The model presented by Suklje (1957), where the relationship between effective stress, void ratio and strain rate defined the consolidation curve. This relationship was presented by the set of isotachtes.

Suklje was the first to suggest that the behavior of clay at a one-dimensional compression is governed by a unique relationship between effective stress, void ratio and strain rate. The model developed by Suklje assumes that creep occurs during the entire consolidation process. It thus assumes that primary consolidation and creep effects are not two separate processes, occurring before and after the dissipation of excess pore pressure. Suklje also accounted for the fact that the time dependent
strains are influenced by the thickness of the clay layer, permeability and drainage conditions.

2.3 The Bjerrum model

In 1967 Bjerrum presented a conceptual model, which, in a similar fashion to Suklje’s model, also assumes that primary consolidation and creep strains are not divided into separate processes /Bjerrum 1974/. It should be observed that the model is primarily intended for settlements that have developed for a long period of time, i.e. a period of time in a geological perspective. The engineer however, is normally concerned with a shorter period of time, often 50-100 years or shorter. Consequently, in engineering practice, it is essential that the design takes account of the time delay caused by permeability and the drainage conditions.

Figure 2.3 Diagram describing the conceptual model developed by Bjerrum. Series of parallel time lines describing the compressibility and shear strength of clay, which shows delayed consolidation.
The Bjerrum model was intended to explain the apparent preconsolidation pressure or overconsolidation ratio of virgin clays, resulting from geological ageing. The model also explains settlements and creep effects occurring over time, in spite of the fact that the preconsolidation pressure has not been exceeded. In figure 2.3 the unique relationship between void ratio, pressure (effective stress) and time is represented by a series of parallel time lines on the vertical pressure-void ratio diagram. Bjerrum separated strains into “instants” and “delayed” compression and used “time lines” to model the reduced creep rates resulting from the increased duration of loading.

Figure 2.4 Definition of the two parts of settlements, “instant” and “delayed” compression, compared with “primary” and “secondary” compression illustrated by the broken and the solid line respectively (Bjerrum, 1967).

Figure 2.4 shows how the compression of a clay layer is assumed to develop in time for an applied load if the applied load is transferred instantaneously to the clay structure, i.e. as effective stress. This is termed instant compression and the broken lines curve illustrates how the strains would occur if the pore water in the saturated clay could be disregarded. The subsequent compression, i.e. under unchanged effective stress, is the delayed compression. Due to the viscosity of water the effective stresses will gradually increase when the excess pore pressure dissipates and consequently compression will occur along the solid line.
Bjerrum (1967) also stated that there is an obvious relation between preconsolidation pressure and undrained shear strength. The relation is assumed to remain unchanged at changing void ratio (or strain). Hence, a decrease in void ratio, or increasing strains, increases the undrained shear strength. The magnitude of the overconsolidation ratio, OCR, depends, according to Bjerrum, on the plasticity of the clays and its geological history.

2.4 The creep parameter $C_\alpha$ and $\alpha_s$

A widely used parameter for describing the creep behavior of clay is the secondary compression index, $C_\alpha$, defined as (according to Taylor):

$$C_\alpha = \frac{\Delta e}{\Delta \log(t)}$$  \hspace{1cm} (2.5)

where $e$ = void ratio

The creep parameter that is commonly used in Sweden, the coefficient of secondary consolidation, $\alpha_s$, relates to the secondary compression index. The only difference in the definition of the two parameters is that is described $C_\alpha$ as a function of strain, $\varepsilon$ and $\alpha_s$ as a function of void ratio, $e$ /Larsson.1986/. The relationship between the two creep parameters can be expressed as:

$$\alpha_s = \frac{C_\alpha}{1 + e_0}$$  \hspace{1cm} (2.6)

where $1 + e_0$ = the specific volume, $V$ $e_0$ = initial void ratio

The coefficient of secondary compression, $\alpha_s$, is thus defined as:

$$\alpha_s = \frac{\Delta e_{cr}}{\Delta \log(t)}$$  \hspace{1cm} (2.7)
Where \( \alpha_s \) = coefficient of secondary compression

\( \varepsilon_{cr} \) = creep strain

\( t \) = time

The creep behavior is often described by the coefficient of secondary compression, \( \alpha_s \), as a function of strain. Figure 2.6 shows a general model of \( \alpha_s \) and its variation with strain. The coefficient \( \beta_{\alpha s} \) define the change in \( \alpha_s \) with increasing strain /Larsson.1986/.
2.5 The time resistant concept

Another parameter that described the creep behavior is the time resistance, \( R \), introduced by Janbu (1969). If an applied stress is to be considered as an action, then the stress will be considered as a reaction. In the case of creep, the time will be considered as an action and the creep strain is its reaction. This relationship is defined as:

\[
R = \frac{dt}{d\varepsilon} \tag{2.8}
\]

where \( R = \) time resistance [s]
\( \varepsilon = \) strain

In laboratory tests it has been found that the time resistance of clays increases about linearly with time, as is illustrated in Figure 2.7, and can be expressed as:

\[
\frac{dR}{dt} = r_s \tag{2.9}
\]

where \( r_s \) is the time resistance number.

It can be seen from Figure 2.7 that after a certain time \( t_0 \) the time resistance is assumed to increase linearly with time /Svanø & Christensen 1991/. Thereafter the relation may be expressed:

\[
R = r_s(t - t_r) \tag{2.10}
\]

where \( t = \) time
\( t_r = \) reference time
The creep strain rate $\varepsilon$ at time is equal to the inverse of the time resistance $R$:

$$\varepsilon_{cr} = \frac{\partial \varepsilon_{cr}}{\partial t} = \frac{1}{R} \frac{1}{(t-t_r)}$$  \hspace{1cm} (2.11)

where $\varepsilon_{cr} = \text{creep strain rate [1/s]}$

$\varepsilon_{cr} = \text{creep strain}$

By integration of equation (2.11) from $t_0$ to $t$, the strain due to creep can be expressed as:

$$\Delta \varepsilon_{cr} = \frac{1}{r_s} \int_{t_0}^{t} \frac{dt}{r_s(t-t_r)} = \frac{1}{r_s} \ln \frac{t-t_r}{t_0-t_r}$$  \hspace{1cm} (2.12)

where $t_0 = \text{time when } R-t \text{ curve approaches a straight line}$

From equation (2.12), the time resistance number, $r_s$, can hence be defined as:
\[ \frac{1}{r_s} = \frac{\partial \varepsilon_{cr}}{\partial \ln t} \]  

(2.13)

Finally the relationship between the time resistance and the coefficient of secondary consolidation is given by:

\[ \alpha_s = \frac{\partial \varepsilon_{cr}}{\partial \log(t)} = \frac{\partial \varepsilon_{cr}}{\partial \ln(t)} \cdot \frac{\partial \ln(t)}{\partial \log(t)} = \frac{\partial \varepsilon_{cr}}{\partial \ln(t)} \cdot \ln 10 \]  

(2.14)

\[ \alpha_s = \frac{\ln 10}{r_s} \approx \frac{2.3}{r_s} \]  

(2.15)

### 2.6 Relationship between parameters for primary and secondary consolidation

A parameter commonly used worldwide to describe the compression behavior of clay for effective stresses greater than the preconsolidation pressure is the compression index, \( C_c \), which is defined as:

\[ C_c = \frac{\Delta e}{\Delta \log \sigma'} \]  

(2.16)

where \( e \) = void ratio

Mesri and Godlewski (1977) claimed that there is a unique relationship between \( C_\alpha \) and \( C_c \) that holds true for any type of soil and that will be valid for any kind of combinations of time, effective stress and void ratio:

\[ \frac{C_\alpha}{C_c} = \text{constant} \]  

(2.17)

For a majority of inorganic soft clays the relationship equals (Mesri and Castro, 1987):
\[
\frac{C_a}{C_c} = 0.04 \pm 0.01
\] (2.18)

In 1985 Janbu defined the relation between the *modulus number*, \( m \), and *time resistance number*, \( r_s \), as:

\[
\frac{C_a}{C_c} = \frac{m}{r_s}
\] (2.19)

where

\[
m = \frac{M(\sigma')}{\sigma'^2}
\]

\( M(\sigma') = \) oedometer modulus [kPa]

\( \sigma' = \) effective stress [kPa]

The stiffness of the clay is assumed to increase linearly with stress in the normally consolidated domain, i.e., \( M = m . \sigma' \). This is in accordance with the concept of Janbu’s tangent modulus.

As has been shown, the three creep parameters described in this section are strongly related to each other, despite the fact that there can be some significant differences.

**Appendix 1:** The relationship between effective stress, strain and strain rate
The effect of temperature on the compressibility
Determination of the creep parameter from CRS tests
3 OEDOMETER TESTS-EXPERIMENTAL RESULTS

3.1 Operating method

The Casagrande oedometer test is most widely used. The apparatus (see figure 3.1) consists of a cell which can be placed in a loading frame and loaded vertically. In the cell the soil sample is laterally restrained by a steel ring, which incorporates a cutting shoe used during specimen preparation. The top and bottom of the specimen are placed in contact with porous discs, so that drainage of the specimen takes place in the vertical direction when vertical stress is applied; consolidation is then one-dimensional.
To run this test a standard procedure is to follow. In this procedure the specimen is subjected to a series of pre-selected vertical stresses each of which is held constant while dial gauge measurements of vertical deformation of the top of the specimen are made, and until movements cease (normally 24 h and several weeks for long-time test). Dial gauge readings are taken at standard intervals of time after the start of the test (i.e. 0, 6, 15 and 30s, 1, 2, 4, 8, 15, 30 and 60mm, 2, 4, 8 and 24h). At the same time that the first load is applied, the oedometer cell is flooded with water, and if the specimen swells the load is immediately increased through the standard increments until swelling ceases.

There is different kind of oedometer tests (Increment load IL, constant rate of strain…). The one I have carried out is the standard incremental loading test. The principle is to proceed with applying at each step a double load increment than the current one. For each phase values (height of the sample or strain) are checked and plotted. The stabilisation of the settlements indicates us that a new load increment is to be put. To study the behavior of clay in the long run, tests were carried out (for the last load increment) from 30 to 100 days."

Figure 3.2 Oedometer test in the laboratory
3.2 Results processing – Curves fitting

For this project, I have carried out a long duration oedometer test, Otaniemi 4702, and I have processed also the results of former oedometer tests. Here are the tests considered, some characteristics and their references:

<table>
<thead>
<tr>
<th>Reference number</th>
<th>Sampling site</th>
<th>From (load)</th>
<th>To (load)</th>
<th>( \sigma_1 ) [kPa]</th>
<th>Original depth</th>
<th>Sample type</th>
<th>Duration-load step ( \sigma_1 ) [days]</th>
</tr>
</thead>
<tbody>
<tr>
<td>806</td>
<td>Otaniemi</td>
<td>6,25</td>
<td>200</td>
<td>25</td>
<td>2,32 – 2,35</td>
<td>2</td>
<td>70</td>
</tr>
<tr>
<td>116</td>
<td>Perno</td>
<td>12,5</td>
<td>800</td>
<td>25</td>
<td>1,75 – 1,77</td>
<td>1</td>
<td>55</td>
</tr>
<tr>
<td>21D1</td>
<td>Taasia</td>
<td>100</td>
<td>1600</td>
<td>100</td>
<td>4,42 – 4,45</td>
<td>2</td>
<td>90</td>
</tr>
<tr>
<td>26B1</td>
<td>Taasia</td>
<td>50</td>
<td>1600</td>
<td>100</td>
<td>3,47 – 3,50</td>
<td>2</td>
<td>100</td>
</tr>
<tr>
<td>4452</td>
<td>Vanttila</td>
<td>3,57</td>
<td>84</td>
<td>42</td>
<td>2,64 – 2,67</td>
<td>3</td>
<td>68</td>
</tr>
<tr>
<td>4453</td>
<td>Vanttila</td>
<td>3,57</td>
<td>84</td>
<td>42</td>
<td>1,64 – 1,66</td>
<td>3</td>
<td>67</td>
</tr>
<tr>
<td>4072</td>
<td>Otaniemi</td>
<td>5,35</td>
<td>342,4</td>
<td>42,8</td>
<td>1,90 – 1,92</td>
<td>3</td>
<td>7</td>
</tr>
</tbody>
</table>

Sample type 1: \( h_0 = 1,88 \) cm; \( A = 45,7 \) cm\(^2\)
Sample type 2: \( h_0 = 2 \) cm; \( A = 20 \) cm\(^2\)
Sample type 3: \( h_0 = 1,5 \) cm; \( A = 13,82 \) cm\(^2\)

(See Appendix 2, Sampling)

3.2.1 Determination of the coefficient of consolidation \( c_v \), the coefficient of secondary compression \( C_a \), the end of primary consolidation time \( t_{EOP} \) and the height at the end of primary consolidation \( H_{EOP} \)

The results of each loading stage of an oedometer test are normally plotted in a chart representing the dial gauge readings either as a function of square root of elapsed time, or as a function of the logarithm of elapsed time. The coefficient of consolidation \( (c_v) \) used in calculations of settlement can be obtained from these curves, using Taylor and Merchant’s method, or Casagrande’s method respectively. \( C_a \) and the characteristic EOP parameters are also obtained thanks to these curves.
Example:
For the test 4452 on the sample from Vanttila site here is how the data are determined (end of primary consolidation EOP, consolidation coefficient $c_v$, $C_\alpha$):

For each load step we plot the height-time (log(t):Casagrande; sqrt(t):Taylor) curve.

Figure 3.3 Determination of the characteristic EOP parameters, $C_v$ and $C_\alpha$ - Fifth

Load step: 42,4 kPa of Vanttila 4452

For the load step $\sigma_1$ we assess the value of $C_\alpha$ and $c_v$ (with the Casagrande's and the Taylor's method):

### 3.2.1.1 Casagrande’s method

The logarithmic method consists in plotting the deformation-time dependency in a semi-logarithmic scale. The consolidation coefficient itself is determined from the relation:

$$c_v = \frac{T_{50} \cdot H^2}{t_{50}}$$  \hspace{1cm} (3.1)

where $T_{50}$ is a time factor corresponding to 50% primary consolidation and where $t_{50}$ is the time necessary for reaching 50% consolidation.

The time factor $T_{50} = 0.197$. For a sample drained at both sides, the height $H$ equals half of the sample’s height.

$$c_v = \frac{0.197 \cdot H^2}{t_{50}}$$  \hspace{1cm} (3.2)
In order to be able to determine $t_{50}$, we must first find the beginning of primary consolidation and the inflexion point of the medium part of the consolidation curve and a line running along the straight section of the last part of the curve. This point is considered to be the end of primary and the beginning of secondary consolidation. As can be seen from the figure 3.4, the time at 50% consolidation is given by the intersection point of a parallel line to the axis x and the consolidation line, the parallel line with the axis x being exactly in the middle of deformation, between the beginning and the end of primary consolidation. The beginning of primary consolidation may be found e.g. by plotting the time 16t and its quarter 4t, and it further holds true that the distance between these two times on the vertical axis equals $1/2$ of total deformation reached in the time 16t from the beginning of primary consolidation.

Here with the Casagrande’s method: $c_v = 0.13 \, \text{m}^3/\text{a}$
N.B:
The last part of the some curves plotted in Figure 3.5 shows an increased slope. This can be explained by local stress relaxation and hence an increase in the heights of energy links of the slip units. This is akin to work-hardening, e.g. as in metals. Indeed a critical number of slip units is reached and domains formation stops leading to an accelerating creep rate followed by complete failure. But this phenomenon can also be explained by the formation of high local stress point which makes the energy barriers among slip units decreased, this outweighs the creep effects due to domains formation /Pusch 1978/. Modelling this behavior has been studied in chapter 5.

**Figure 3.5** Strain-log(t) curves of the different studied tests

**Figure 3.6** Change in the creep slope
3.2.1.2 Taylor’s method

Taylor’s method is very commonly used. Time is plotted on the horizontal axis in the form of a root of t, while deformation is plotted on the vertical axis. The intersection point of the tangent to the linear section of the consolidation curve with the vertical axis is considered to be the beginning of primary consolidation. A line with a tangent 1.15 times greater than the above-mentioned tangent is led through the point ds. The method presumes that this line intersects the consolidation curve at a point which corresponds to 90% consolidation. Numerical solution of uniaxial consolidation may be performed analytically by using Fourier series (Taylor, 1948). It is presumed that the experimental curve for the point A is identical to the theoretical curve (A representing 90% consolidation).

Thus, if we know the time factor we may determine the consolidation coefficient from the relation 3.3:
\[ c_v = \frac{0.848 \cdot H^2}{t_{90}} \]  

(3.3)

where \( H \) is the half of the sample's height in [m]; \( t_{90} \) is the time at reaching 90% consolidation in [s] and \( T_{90} = 0.848 \) is the time factor at this same time.

A condition of great importance in using Taylor’s method is that the test sample should be fully saturated.

Here with Taylor’s method: \( c_v = 0.22 \, \text{m}^2/\text{a} \)

### 3.2.2 Determination of the preconsolidation pressure \( \sigma'_p \), the compression index \( C_c \) and the swelling index \( C_s \)

The results of all the oedometer load stages are normally combined in one graph of void ratio as a function of the logarithm of effective pressure (figure below), constructed on the basis of the calculated void ratios at the end of each of the load stages (or with the EOP value). These results are also used to calculate the coefficient of compressibility (\( m_v = \Delta e/(1 + e_0) \cdot (1/\Delta p) \), where \( \Delta e \) is the void ratio change for a pressure change \( \Delta p \) which is used to predict the magnitude of settlement. This is carried out for each load stage. Coefficient of compressibility results are seriously affected by sample disturbance in soft or sensitive clays, and by sample size effects in hard clays and soft rocks.

We can now model the behavior of clay with load with two methods more or less useful and accurate. The first model rely on Janbu’s equation and aims at modelling the bend of the curves plotted on the \( e - \sigma_1 \) chart. To proceed we use TAMO (in-plant program) from which we get the parameter \( m_1, \beta_1, m_2, \beta_2 \) characteristic parameters for Janbu’s model of the consolidation. The second model, more classical, uses two straight lines, the coefficient of which are \( C_c \) and \( C_s \) (or \( C_r \)). This modelling is less accurate and so on not reliable concerning determination of the preconsolidation pressure.
The trend curves stick more to the real phenomenon when modelled by Janbu’s equation taking into account the bend of the curve. That’s why we prefer using this model and proceeding as proposed by A.Aalto & M.Lojander & O.Ravaska to determine the preconsolidation pressure /A.Aalto & M.Lojander & O.Ravaska 2004/. However the classical modelling is necessary because the parameters got from this model are of use in many consolidation model and FEM software (e.g. PLAXIS).

Figure 3.8 Models comparison of clay’s behavior
We can now determine the preconsolidation pressure thanks to these charts obtained with Janbu’s modelling.

![Graph](image)

*Figure 3.9 Preconsolidation pressure determination on Otaniemi 4702*

The preconsolidation pressure is here 31 kPa. Note that the value is widely influenced anyway by the point chosen to model the trendline.

At the end of the test the sample is weighed then dried and weigh again thus we can assess the water content of the sample and its void ratio.

N.B: In order to proceed the numerical modelling of the oedometer test we need to get the values of the Cam-Clay swelling index $\kappa$, the Cam Clay compression index $\lambda$, and the modified creep index $\mu$. This has been done manually by converting the parameters as explained in chapter 4.

Appendix 2: Sampling
- Classification data
- Other tests
4 NUMERICAL MODELLING: PLAXIS SIMULATION OF OEDOMETER TESTS

4.1 The Plaxis Soft Soil Creep Model (Buisman model)

4.1.1 Model’s equation

The principle of the calculation is based on Buisman creep model. Of course this model has been improved all along the year to come to this one. It has been improved thanks to the work of researchers like Bjerrum, Garlanger or Mesri. Eventually the model was implemented in Plaxis in 1998 thanks to the work of Vermeer et al. and Neher & Vermeer /PLAXIS-material models manual/.

The basic equation of the model is the following one:

\[
\varepsilon^H = \varepsilon_c^H - C \cdot \ln \left( \frac{\tau_c + t'}{\tau_c} \right)
\]

Where \( \varepsilon_c^H \) is the logarithmic strain defined as

\[
\varepsilon^H = \ln \left( \frac{V}{V_0} \right) = \ln \left( \frac{1 + e}{1 + e_0} \right)
\]

And

\[
C = \frac{C_\alpha}{(1 + e_0) \cdot \ln 10}
\]

is a modification of the compression index

\[ t' \] is the effective creep time: \( t' = t - t_c \) (see fig 4.12)

and \( \tau_c \) the time up to the strain rate starts decreasing (we can however assess \( \tau_c = t_c \) )
Figure 4.1 Consolidation and creep behaviour in standard oedometer test

From this model are adapted the two main equations used to compute the results:

\[ \varepsilon = \varepsilon^c + \varepsilon^c = -A \ln \left( \frac{\sigma'}{\sigma_0'} \right) - B \ln \left( \frac{\sigma_{pc}}{\sigma_{p0}} \right) - C \ln \left( \frac{\tau_c + t'}{\tau_c} \right) \]  \hspace{1cm} (4.3)

And the differential law following:

\[ \dot{\varepsilon} = \dot{\varepsilon}^c + \dot{\varepsilon}^c = -A \frac{\sigma'}{\sigma'} - C \left( \frac{\sigma'}{\sigma_p} \right)^\frac{B}{C} \] \hspace{1cm} (4.5)

In which $A$, $B$, and $C$ are customised constants described as following:

\[ A = \frac{C_r}{(1 + e_0)^\ln 10} \] \hspace{1cm} (4.6)

\[ B = \frac{C_c - C_r}{(1 + e_0)^\ln 10} \] \hspace{1cm} (4.7)

\[ C = \frac{C_\alpha}{(1 + e_0)^\ln 10} \] \hspace{1cm} (4.8)
And
\[ \sigma' \] the final effective loading pressure
\[ \sigma_0' \] the initial effective pressure before loading
\[ \sigma_{pc} \] the preconsolidation pressure at the end of consolidation
\[ \sigma_{p0} \] the preconsolidation pressure before loading

### 4.1.2 Particular model’s parameters

The parameters used in Soft-Soil-Creep model are not the one we usually find in the literature. Most of the time, using Janbu’s model (cf. 3.3.2) is more accurate to simulate the behavior of the clay. However we are using here parameters resulting from the classical model (with a straight line):

- Modified compression index, \( \lambda^* \)

\[
\lambda^* = \frac{\lambda}{1 + e_0}
\]  

(4.9)

See Figure 4.2 below.

- Modified swelling index, \( \kappa^* \)

\[
\kappa^* = \frac{\kappa}{1 + e_0}
\]  

(4.10)

Usually the value of kappa is determined by the same method. However the different values used to plot the trendline are extracted thanks to an unloading-reloading process. When such a process is not carried out we can assess the value of \( \kappa \) in the range \([ \frac{\lambda}{10} ; \frac{\lambda}{5} \] \).

\( \kappa \) and \( \lambda \) value are both extracted from the ln\( \sigma_1 \)-volumetric strain plot (v=1+e).
Figure 4.2 Determination of lambda and kappa parameters

They are then converted into $\kappa^*$ and $\lambda^*$ as explained before-mentioned.

- Modified creep index, $\mu^*$

$$\mu^* = \frac{C_\alpha}{(1 + e_0).\ln10}$$

(4.11)

The secondary compression index, $C_\alpha$, is extracted from the oedometer test data processed as explained below. See Figure 4.3.
4.1.3 Parameters’ influences

- Modified compression index, $\lambda^*$
  $\lambda^*$ is an equivalent parameter to $C_c$. It means that the higher the parameter is the steeper is the second part of the curve in the Casagrande construction.

- Modified swelling index, $\kappa^*$
  $\kappa^*$ is an equivalent parameter to $C_s$. The modified swelling index is of great importance when it deals with excavating or clearing away. But it is also of importance when modelling oedometer tests. Indeed the swelling compression index is one of the main parameter that enables us to assess the instant compression. The higher $\kappa^*$ is the bigger instant compression is. This phenomenon is more noticeable when modelling drained materials.
• Modified creep index, $\mu^*$

$\mu^*$ is an equivalent parameter to $C_a$. Thus the higher this coefficient is the steeper the final part of the slope is.

• Permeability, $k$

The permeability influences widely the delay of the compression. Indeed a high value of $k$ means that the water can circulate easily in the soil enabling the pore water pressure to dissipate quickly. On the contrary a low value of $k$ will prevent pore water pressure to dissipate that quickly. On the plot we can notice this phenomenon by a shift in time.

4.2 Calculated/Observed data comparison for the different oedometer tests.

4.2.1 Oedometer tests simulation

In order to model properly the oedometer test we use these specific features.

• axisymmetric model.
• horizontal and vertical displacement blocked at the foot of the sample.
• horizontal displacement blocked at the sides of the sample.
• water level set at the upper side of the sample (saturated sample).
• upper and lower side drained.
• material behavior: Undrained.
• side boundaries closed for consolidation and water flow.
• application of the load trough a infinitely rigid plate (very high young modulus)
• instant application of the load then consolidation phase as long as desired.
N.B:
The mesh generation is not of big importance in this model as the shape is simple. A coarse mesh is thus accurate enough.

4.2.1.1 Otaniemi 4702

4.2.1.1.1 Parameters

- Dimensions of the sample:
  - $H_{\text{init}} = 15 \text{ mm}$
\( \text{o} \quad A = 1382 \text{ mm}^2 \)

- \( \sigma_1 = \sigma \text{ applied} = 42.8 \text{ kPa} \)
- \( \sigma_{10} = \sigma \text{ applied at the previous load step} = 21.4 \text{ kPa} \)
- \( h_0 = \text{height of the sample at the end of the previous load step} = 14,265 \text{ mm} \)

- \( k = 3.65 \times 10^{-5} \text{ m/day} \)
- \( e_0 = 2.12 \)
- \( POP = |\sigma_p - \sigma_{yy}^0| = |25 - 0| = 25 \text{kPa} \)

- \( c = 2 \text{ kPa} \)
- \( \varphi = 24^\circ \)
- \( \psi = 0^\circ \)

- \( \gamma_{sat} = 15.45 \text{ kN/m}^3 \)
- \( \gamma_{unsat} = 8.64 \text{ kN/m}^3 \)

### 4.2.1.1.1 Modified compression index, \( \lambda^* \)

For this modelling a study on the influence of the method to get the lambda and kappa value has been carried out.

Indeed to get these values we plot the \( \sigma_1 = n\text{(voumetric strain} = 1 + e) \) but the value of the settlement can be taken at different time and give thus different value of the slope (\( \lambda \)). One has plotted the value of the volumetric strain for each load step at: the end of the load step (7 days), 1 days and 2.4 hour. Thus we have obtained different values of lambda depending on the way to process the test’s data. / Perrone. 1998/

If we plot the time line for this test according to Bjerrum’s concept we obtain Figure 4.6 below:
Figure 4.6  Bjerrum time lines observed for 4702 oedometer test

Figure 4.7  Assessment of the lambda coefficient in the course time resulting from Bjerrum’s chart

This coefficient ($\lambda$) decreases all the more if you assess its value late in time during the settlement of a load stage as we can see on Figure 4.8:
4.2.1.1.1.2 Modified swelling index, $\kappa^*$

The second aspect of the study regards the way to assess the value of $\kappa$. Indeed the unloading curve is not really a straight line so if we only take the very first points to assess the slope, the value of $\kappa$ will be lower than if we regard every points of the unloading stage (see figure 4.9).

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure4.8.png}
\caption{Evolution of the lambda value with time}
\end{figure}
Figure 4.9 Influence of the points considered to model the slope of the recompression line

Eventually the set of parameters $\lambda - \kappa$ can be summed up in this table:

<table>
<thead>
<tr>
<th>Settlement at final time</th>
<th>$\kappa$ init</th>
<th>$\kappa$ all</th>
<th>$\lambda^*$</th>
<th>$\kappa^*$</th>
<th>$\lambda / \kappa$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Settlement at t=1 day</td>
<td>0.2877</td>
<td>0.0578</td>
<td>9.22.E-2</td>
<td>1.05.E-2</td>
<td>8.78</td>
</tr>
<tr>
<td>Settlement at t=2,4H</td>
<td>0.2815</td>
<td>Default</td>
<td>9.02.E-2</td>
<td>1.05.E-2</td>
<td>8.6</td>
</tr>
</tbody>
</table>

4.2.1.1.3 Modified creep index, $\mu^*$ ($C_\alpha$)

The goal of this study is to uproot errors coming from subjective plotting of $C_\alpha$ trendline. According to Mesri and Godlewski, the value of the ratio Ca/Cc should be constant and equal to 0.04±0.01. In this study we will try to estimate the value of $C_\alpha$ after a one day-long test, the value after a 7 day-long test (value obtained by assessing the slope
regarding the height at 6 days and 7 days) and eventually the value of $C_\alpha$ that best fits to the entire curve.

Example: Load step 42,8kPa

![Graph showing load step 42,8kPa with 1 day assessment: $C_\alpha = 0.67$ and 7 days assessment: $C_\alpha = 0.48$]

**Figure 4.10** $C_\alpha$ assessment.

**Table 4.2** Set of parameters $C_\alpha$

<table>
<thead>
<tr>
<th>Load step (kPa)</th>
<th>$C_\alpha$ 7day (%)</th>
<th>$C_\alpha$ 1day (%)</th>
<th>$C_\alpha$ 7day (%)</th>
<th>$C_\alpha$ 1day (%)</th>
<th>$C_\alpha$ 7day best fitted slope (%)</th>
<th>$C_\alpha$ 7day best fitted slope (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>42.8</td>
<td>0.48</td>
<td>0.01498</td>
<td>0.67</td>
<td>0.0209</td>
<td>0.68</td>
<td>0.021216</td>
</tr>
<tr>
<td>85.6</td>
<td>0.2</td>
<td>0.00624</td>
<td>0.82</td>
<td>0.02558</td>
<td>0.68</td>
<td>0.021216</td>
</tr>
<tr>
<td>171.2</td>
<td>0.52</td>
<td>0.01622</td>
<td>0.73</td>
<td>0.02278</td>
<td>0.76</td>
<td>0.023712</td>
</tr>
<tr>
<td>342.4</td>
<td>0.53</td>
<td>0.01654</td>
<td>0.6</td>
<td>0.01872</td>
<td>0.51</td>
<td>0.015912</td>
</tr>
</tbody>
</table>

N.B: “Best fitted slope” is obtained regarding all points of the test and plotting the curves.

We should now assess the value of parameter $\lambda$ at each stage of the test, to be able to determine its variation with the course of time and thus the variation of $C_\alpha / C_c$ ratio.

To assess the value of the $\lambda$ coefficient at each step we use a linear regression on the two points (before and at the load step considered):
The values of $\lambda$ are acquired this way for each load step. Here is the table compiling the values:

<table>
<thead>
<tr>
<th>Load step [kPa]</th>
<th>42.8</th>
<th>85.6</th>
<th>171.2</th>
<th>342.4</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\lambda$</td>
<td>0.2371</td>
<td>0.3139</td>
<td>0.3049</td>
<td>0.2734</td>
</tr>
</tbody>
</table>

Here are the results of the study (plotted with $C_\alpha/C_c$ value obtained in Table 4.2):
One can notice that the value of $C_\alpha/C_c$ is far from being constant all along the test. However for the value “best fitted after 7 days” and “1 day test” the ratio stays in the range predicted by Mesri and Castro (0.04±0.01).

Now let’s try to get a constant ratio. Let’s study the case “best fitted curve” and try to improve our method to plot the slope of the secondary consolidation.

First we calculate the average value of $C_\alpha/C_c$:

$$C_\alpha/C_{c_{average}} = \frac{0.03886 + 0.02935 + 0.03377 + 0.02528}{4} = 0.03182$$

If we try to follow Mesri’s assumption we can get the value of $C_\alpha$ thanks to the value of lambda checked:

<table>
<thead>
<tr>
<th>Load step (kPa)</th>
<th>Cc (local)</th>
<th>Calpha resulting</th>
<th>Calphae resulting (%)</th>
<th>Calphae observed</th>
<th>Errors plotting the slope (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>42.8</td>
<td>0.545943</td>
<td>0.017372</td>
<td>0.556791791</td>
<td>0.68</td>
<td>-22.1282</td>
</tr>
<tr>
<td>85.6</td>
<td>0.722781</td>
<td>0.022999</td>
<td>0.737144426</td>
<td>0.68</td>
<td>7.752134</td>
</tr>
<tr>
<td>171.2</td>
<td>0.702058</td>
<td>0.022339</td>
<td>0.716009351</td>
<td>0.76</td>
<td>-6.14387</td>
</tr>
<tr>
<td>342.4</td>
<td>0.629527</td>
<td>0.020032</td>
<td>0.642036591</td>
<td>0.51</td>
<td>20.56528</td>
</tr>
</tbody>
</table>

Let’s see the difference induced by the correction of the slopes on the Casagrande’s construction for some load steps.

![Figure 4.13 C_\alpha slope, best fitted/corrected (Load step 42.8kPa)](image-url)
Such apparently tiny differences can be of importance when it deals with long term settlements. For the load step 42.8 kPa, secondary consolidation strain is about 20%
bigger when plotted without correction after 100 hours of consolidation (eventually, for the simulation, $\mu^*$ has been set to 2.95E-3).

4.2.1.1.2 Results

**Figure 4.17** Computed/observed settlement of the 4702 oedometer test's sample $\lambda$ (values at 7 days) and $\kappa$ obtained as described above

**Figure 4.18** Computed/observed settlement of the 4702 oedometer test's sample $\lambda$ (values at 1 day) and $\kappa$ obtained as described above
Figure 4.19  Computed/observed settlement of the 4702 oedometer test’s sample / λ (values at 1/10day) and κ obtained as described above

If we compare now the difference in the calculated curves obtained with the different value of λ (values acquired by plotting the reading of the settlement at t=7days, t=1day and t=2,4H) we can notice that the difference between those curves is not noteworthy.

Figure 4.20  Comparison between the computed settlement of the 4702 oedometer test’s sample; κ = cst, λ function of acquisition day values
Comments:

- Lambda values depends slightly on the time acquisition of the settlement values as we have seen but one should notice that these values are much more affected by the points used to get the lambda value from the experimental test results.

- The real value of kappa is hard to determine as it's not the only parameter which might be discussed in the modelling. One can suppose that the most correct value is situated between $\kappa^{\text{all}}$ and $\kappa^{\text{init}}$. Anyway as we have said before the curve is modelled by a straight line in this model which let us think that there's no absolutely right value.

- The values of the preconsolidation pressure and the permeability have been set in order to chock the model and stick as close as possible to the reality. The chocking has anyway not been exposed as it has not been subject to study. The range was given for the permeability by the Taylor’s and Casagrande’s assessment of the value [2,29.E-5m/day ; 3,65.E-5m/day]. For the preconsolidation pressure the range was given thanks to the different time acquisition curves: [24kPa ; 31kPa].

4.2.1.2 Otaniemi 806

4.2.1.2.1 Parameters

- Dimensions of the sample:
  - $H_{\text{init}} = 20$ mm
  - $A = 2000$ mm$^2$

- $\sigma_1 = \sigma$ applied = 25 kPa

- $\sigma_{\text{10}} = \sigma$ applied at the previous load step = 12,5 kPa

- $h_0 = \text{height of the sample at the end of the previous load step} = 19,361$ mm

- $\lambda^* = 0,24257$

- $\kappa^* = 1,0197.E-2$

- $\mu^* = 9,728.E-3$

- $k = 3,162.E-5$ m/day
• $e_0 = 3.6$
• $POP = |\sigma_p - \sigma_{yy}^0| = |12.5 - 0| = 12.5kPa$

• $c = 2$ kPa
• $\varphi = 24^\circ$
• $\psi = 0^\circ$

• $\gamma_{sat} = 13.6$ kN/m$^3$
• $\gamma_{unsat} = 5.935$ kN/m$^3$

4.2.1.2.2 Results

![Oedometer test: Otaniem 806](image)

Observations:

• The second part of the slope ($\lambda^*$) seems to be acceptable (slope as steep as the slope observed)
• The end of primary consolidation seems a little bit delayed actually.
• The last part of the curve characterized by an increase of the slope is not taken into account in the PLAXIS Soft-Soil-Creep model.
**Figure 4.22**  Computed/observed strain of the 806 oedometer test’s sample

Error at 70 days [%]  27.6
Note that, the actual slope change makes this error grow consequently with time.

About the interest of plotting the curve Epsilon-time:
The height of the sample can’t be settled in the simulation at the accurate value of 19,361mm. As the value assigned is 19 mm the settlement obtained is thus very close but not exactly the same as for a sample of 19,361mm high. The relative value Epsilon enables us to keep apart this source of error.

N.B: Here are presented the results of this two oedometer tests. Simulation of the other oedometer tests can be found in the Appendix 3.

Appendix 3: Taasia 21D1
Taasia 26B1
Vanttila 4452
Vanttila 4453
Perno 116
Suurpelto 4532
Suurpelto 4533
4.3 Analysis

What kind of clay behavior can we simulate with PLAXIS model:

Table 4.5 Validity of PLAXIS’ Soft-Soil-Creep Model for the different tests

<table>
<thead>
<tr>
<th>Test</th>
<th>Instant compression</th>
<th>Part of the curve modelling primary consolidation</th>
<th>Part of the curve modelling creep</th>
<th>Change in the slope of creep (increasing $C_\alpha$)</th>
<th>Final error acceptable</th>
<th>Can be simulated with plaxis soft soil model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Otaniemi 806</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>YES</td>
<td>NO</td>
<td>NO</td>
</tr>
<tr>
<td>Taasia 21D1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>NO</td>
<td>NO</td>
<td>YES</td>
</tr>
<tr>
<td>Taasia 26B1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>NO</td>
<td>YES</td>
<td>YES</td>
</tr>
<tr>
<td>Vanttila 4452</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>NO</td>
<td>YES</td>
<td>YES</td>
</tr>
<tr>
<td>Vanttila 4453</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>YES</td>
<td>YES</td>
<td>YES</td>
</tr>
<tr>
<td>Perno 116</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>YES</td>
<td>NO</td>
<td>-</td>
</tr>
<tr>
<td>Suurpelto 4532</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>YES</td>
<td>NO</td>
<td>NO</td>
</tr>
<tr>
<td>Suurpelto 4533</td>
<td>3</td>
<td>3</td>
<td>2</td>
<td>NO</td>
<td>NO</td>
<td>NO</td>
</tr>
<tr>
<td>Otaniemi 4702</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>NO</td>
<td>YES</td>
<td>YES</td>
</tr>
</tbody>
</table>

(1) good accuracy of the model, stick to actual behavior
(2) different but acceptable
(3) non acceptable

One can note that all the tests can’t be simulated properly thanks to PLAXIS model. For those that can’t be simulated, one should get back to classical modelling.
5 CLASSICAL MODELLING OF OEDOMETER TESTS

5.1 The Asoaka method (1978)

Asaoka method is a method to determine the ultimate primary consolidation. The biggest advantage of the method is its simplicity. Indeed no soil properties are required to determine with this method the ultimate primary consolidation /Stapelfeldt 2000/.

Asaoka admitted that one-dimensional consolidation settlements at certain time intervals could be described as a first order approximation:

\[ S_n = \beta_0 + \beta_1 S_{n-1} \]  \hspace{1cm} (5.1)

Where \( S_n \) is the time settlement at time \( t_n \). The time interval \( \Delta t = (t_n - t_{n-1}) \) is constant.

The first order approximation should represent a straight line on a \((S_n \text{ vs. } S_{n-1})\) coordinate. The values of \( \beta_0 \) and \( \beta_1 \) are given by the intercept of the fitted straight line with the \( S_n \)-axis and the slope.

The ultimate primary settlement can be calculated thanks to the expression:

\[ S_{ult} = \frac{\beta_0}{1 - \beta_1} \]  \hspace{1cm} (5.2)

This value is so determined graphically by the intercepting point with 45°-line i.e. when \( S_n = S_{n-1} \).

N.B 1: This method assumes that the soil is homogeneous and the load constant.

N.B 2: To get a correct line it is of major importance to use points of primary consolidation. (points of instant compression and secondary compression are proscribed)
N.B 3: Tan and Chew (1996) exposed in their article that estimation of the ultimate primary consolidation may be corrected depending on the data used to plot the curve (time of consolidation) /Holtz 1991/.

Table 5.1 Validity and correction of the results obtained thanks to Asaoka method

<table>
<thead>
<tr>
<th></th>
<th>Estimation of $S_{ult}$</th>
<th>Estimation of $c_v$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data 0-30% of consolidation</td>
<td>underestimated</td>
<td>overestimated</td>
</tr>
<tr>
<td>Data 30-60% of consolidation</td>
<td>Underestimated (10%)</td>
<td>Overestimated (30%)</td>
</tr>
<tr>
<td>Data &gt;60% of consolidation</td>
<td>Exact value</td>
<td>Exact value</td>
</tr>
</tbody>
</table>

\[ y = 0.8192x + 0.5182 \]

Fig 5.1 Otaniemi 806: Asaoka method $\Delta t=0.5 \text{ h}$

\[ \beta_0 = 0.5182 \]
\[ \beta_1 = 0.8192 \]
\[ \text{Sult [mm]} = 2.86615 \]

Consolidation: $U[\%] = 63.23\%$
Fig 5.2 Asaoka method $\Delta t=1 \text{ h}$

Consolidation: $U[\%] = 63.14\%$

<table>
<thead>
<tr>
<th>$\beta_0$</th>
<th>0.9503</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta_1$</td>
<td>0.668</td>
</tr>
<tr>
<td>Sult [mm]</td>
<td>2.862349</td>
</tr>
</tbody>
</table>
5.2 The hyperbolic model

This method first proposed by Korhonen (1977) and then improved by Puumalainen (1998) includes modelling of primary and secondary settlement /Stapelfeldt 2000/.

It assumed that the settlement speed is reduced in a hyperbolic manner /Länsivaara/, the time/settlement curve is given as:

\[ S = \frac{t}{\frac{1}{V_0} + \frac{t}{S_f}} \]  

(5.3)

Where  
\( t \)  time  
\( S \)  settlement at time \( t \)  
\( S_f \)  final predicted settlement (= \( S_{ult} + S_s \))  
\( S_{ult} \)  ultimate primary settlement  
\( S_s \)  secondary settlement  
\( V_0 \)  settlement speed at start of observations (\( t=0 \))

This equation can be written this way:

\[ \frac{t}{S} = \frac{1}{V_0} + \frac{t}{S_f} \]  

(5.4)

Thus on the (time/settlement vs time co-ordinate) the inverse of the slope of the straight line denotes the final predicted settlement, \( S_f \), and the interception with time/settlement axis denotes the value \( \frac{t}{V_0} \).

N.B: This method assumes as for the Asaoka method that the soil is homogeneous and the load constant.
The problem with this parameter is that the simulation is not that accurate if we compare to what happen actually. To make it with this we can divide the curve in two parts and assess the parameters for the two parts of the curve with the same method.
5.3 The Buisman model

To predict the settlement Buisman method uses the classical parameter describing secondary compression as explained in chapter 2 /Perrone 1998/.

The settlement is thus calculated from the formula 5.5 below and required to know parameter like the coefficient $\alpha_s$ that we are supposed to extract from experimental results /Vermeer/.

$$S = H_{EOP} \cdot \alpha_s \cdot \Delta \log(t)$$  \hspace{1cm} (5.5)

Where
- $t$ time
- $S$ settlement at time $t$
- $H_{EOP}$ height of the sample at the end of primary consolidation
- $\alpha_s$ coefficient of secondary compression

But this formula is only of use to calculate the secondary compression. One must add the settlement due to primary consolidation. This is made thanks to Brinch-Hansen method.

This method uses this formula (5.6) to assess the settlement:

$$\frac{S}{S_p} = \frac{t^3}{t_{90}^3 + t^3}$$  \hspace{1cm} (5.6)

Where
- $S$ settlement at time $t$
- $S_p$ settlement at the end of the primary consolidation
- $t$ time
- $t_{90}$ time at 90% of the primary consolidation

The value of the $t_{90}$ and $S_p$ are assessed thanks to Taylor’s method (c.f chapter 3). Thus the height of the sample is:
CLASSICAL MODELLING OF OEDOMETER TESTS

$$H = H_0 - S_p \sqrt[6]{\frac{t^3}{t_{90}^3 + t^3}} - \begin{cases} 0 & \text{if } t < t_{EOP} \\ \frac{H_{EOP}}{\alpha_{\Delta \log(t)}} & \text{if } t \geq t_{EOP} \end{cases}$$  \hspace{1cm} (5.7)

Fig 5.5 Otaniemi 806: Buisman (/Brinch-Hansen) model

But with this modelling one can notice that the second part of the secondary compression is not modelled. That’s why another model for clay with such behavior is used, a model considering this phenomenon.
5.4 Anagnosti model

As for Buisman model Anagnosti’s model has been developed to predict settlement due to secondary compression. The primary settlement will therefore be modelled thanks to Brinch-Hansen model (c.f chapter Buisman model).

Anagnosti’s equation:
The model is based on Kelvin’s and Maxwell’s way of modelling the soil (parallel and serie spring/dashpot system) /Tanska 1993/, which enable to extract equation below:

\[ 3K_0 \nu_d \frac{d\varepsilon_z}{dt} + \left( 3\nu_0 \nu_d + \frac{3K_0 \nu^2_d}{G} \right) \frac{d^2\varepsilon_z}{dt^2} + \frac{3\nu_0 \nu^2_d}{G} \frac{d^3\varepsilon_z}{dt^3} = 2K_0 (\sigma_z - \sigma_r) \]  

(5.8)

Where

- \( K_0 \) bulk compressibility modulus
- \( \nu_0 \) coefficient of bulk viscosity
- \( \nu_d \) coefficient of deviatoric viscosity
- \( G \) rigidity modulus
- \( \varepsilon_z \) vertical strain
- \( \sigma_z \) axial stress
- \( \sigma_r \) radial stress

The solution of which is /Anagnosti 1963/:

\[ \varepsilon_z = C_{1V} e^{-\nu_0 t} + C_{2V} e^{\nu_d t} + C_{3V} \]  

(5.9)

With \( C_{1V}, C_{2V}, C_{3V} \) Volume changing constant

Determination of the parameters

- \( K_0 \)

\[ K_0 = \frac{\sigma_z + 2\sigma_r}{3\varepsilon_{zfl}} \]  

with \( \varepsilon_{zfl} = \varepsilon_{zf} + \varepsilon_{zc} \)  

(5.10)
Where

\[ \varepsilon_{zf} \] strain due to secondary consolidation

\[ \varepsilon_{zc} \] strain due to primary consolidation

\[ \varepsilon_{zf} \] total strain

\[ \varepsilon_{zc} \] is determined thanks to Taylor’s method (strain at 100% of the consolidation). Concerning \[ \varepsilon_{zf} \] the best way to assess it, is to plot the \[ t/\varepsilon \]-t chart and to determine the slope of the final part of the curve.

\[
y = 3,7835x + 748,26
\]

Fig 5.6 \[ t/\varepsilon \]-t diagram: Otaniemi 806 oedometer test; \[ \varepsilon_{zf} = 1/3,7835 = 0,264 \]

- \[ \frac{G}{V_{d}} \] and \( C_{2V} \)

By calculating the limits of Anagnosti’s solution we can write:

\[
\ln(A) = \ln\left(\frac{\sigma_z + 2\sigma_c}{3K_0} - (\varepsilon_z - \varepsilon_c)\right) = \ln(-C_{2V}) - \frac{G}{V_{d}t}
\]  
(5.11)

We can therefore obtained \( C_{2V} \) and \( \frac{G}{V_{d}} \) by plotting the \( \ln A \)-t diagram and then assessing the slope and axis intercept of the line modelling the last part of the curve:
Fig 5.7  Otaniemi 806, lnA-t~: $\ln A = e^{-2.5514} = -0.07797$; $G = -0.0006$

- $C_{1V}$

$C_{1V}$ is easily calculated once $C_{2V}$ obtained thanks to this formula resulting from boundary consideration on Anagnosti's solution:

$$C_{1V} = -C_{2V} - \frac{\sigma_z + 2\sigma_r}{3K_0} \quad (5.12)$$

- $\nu_0$

Let's still consider boundary values ($t \to 0$), then $\nu_0$ can be calculated as described below:

$$\nu_0 = \frac{K_0 C_{1V}}{\dot{\varepsilon}_v(t = 0) + \frac{G}{V_d} C_{2V}} \quad (5.13)$$
For example for Otaniemi 806:

\begin{figure}
\centering
\includegraphics[width=\textwidth]{fig5.8.png}
\caption{Otaniemi 806, \( d\varepsilon/dt-t^{-}\): \( \dot{\varepsilon}_v(t = 0) = 0.001963 \Rightarrow \nu_0 = 3212.43 \text{ kPah} \)}
\end{figure}

\( \dot{\varepsilon}_v(t = 0) = 0.001963 \) and so \( \nu_0 = 3212.43 \text{ kPah} \)

N.B:
Acquiring of this parameter is not that reliable and is of great influence on the shape of the predicted curve. Indeed \( \dot{\varepsilon}_v(t = 0) \) can be from simple to double value (changing at the same time the value of \( \nu_0 \) ) depending on the points used for calculation of the Volume changing rate ((t-1;t); (t;t+1); (t-1;t+1)). This modifies consequently the shape of the curve.

\begin{itemize}
\item \( C_{3P} = \frac{\sigma_u + 2\sigma_s}{3K_0} \) \hspace{1cm} (5.14)
\end{itemize}

All the necessary parameters are now known. We can plot the value of the observed and calculated strain (with Anagnosti’s model eq 5.15):
Table 5.2 Parameters for the Anagnosti/Brinch-Hansen modelling

<table>
<thead>
<tr>
<th>Parameter's to Brinch-Hansen's equation</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon_{EOP}$ = 15,753%</td>
<td></td>
</tr>
<tr>
<td>$t_v = 6,54$ h</td>
<td></td>
</tr>
<tr>
<td>$c_v = 0,09$ m².a⁻¹</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameter's to Anagnosti's equation</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_0 = 149,77$ kPa</td>
<td></td>
</tr>
<tr>
<td>$C_{1v} = -0,04109$ h</td>
<td></td>
</tr>
<tr>
<td>$\varepsilon_{zc} = 14,52%$</td>
<td></td>
</tr>
<tr>
<td>$\nu_0 = 3212,43$ kPa.h</td>
<td></td>
</tr>
<tr>
<td>$C_{2v} = -0,07797$ h</td>
<td></td>
</tr>
<tr>
<td>$\varepsilon_{zf} = 26,43%$</td>
<td></td>
</tr>
<tr>
<td>$\frac{G}{\nu_d} = 0,0006$ h⁻¹</td>
<td></td>
</tr>
</tbody>
</table>

\[
\varepsilon = \begin{cases} 
\varepsilon_{EOP} \frac{t^3}{t_{90} + t^3} & \iff t < t_{EOP} \\
\frac{K_0}{C_{1v} e^{\frac{G}{\nu_d}} + C_{2v} e^{\nu_d} + C_{3v}} & \iff t \geq t_{EOP}
\end{cases}
\]  

(5.15)

Fig 5.9 Otaniemi 806: Brinch-Hansen model; Anagnosti model
Anagnosti’s model is, thanks to its accuracy for this particular clay behavior, probably the fittest model to predict settlements. The second part of secondary compression is regarded.
6 CONCLUSION

The aim of this final project was to study the different model and way to model the creep behavior of soft Finnish clay. As a support, oedometer test Otaniemi 806 and Otaniemi 4702 has been processed in this work. They deliver the advantage of showing two different behaviors occurring during secondary consolidation. All along my work here, Test Otaniemi 4702 has been carried out from sampling on the field to the final stage of the oedometer test which has given me an overall view of the laboratory work. Other tests have nevertheless been studied (not as deep as for these one) and can be found attached in appendices.

Plaxis Soft-Soil-Creep model has shown its limits using strictly Buisman model. The way of modelling has been checked and is apparently correct. One can therefore come to the conclusion that the problem comes from the model itself (Buisman model) which doesn’t fit to certain particular clay, e.g. Otaniemi 806. Indeed we expected this insufficiency of the model regarding the equation and the parameter describing the model (linear law with logarithm of time for settlement due to secondary compression).

Otaniemi 806 oedometer test has thus been modelled properly thanks to a classical model with Excel software. Anagnosti’s model has proved here a good accuracy. It achieves to model properly clay the behavior of which shows a second phase (increase of settlement’s rate) in secondary compression. It should supersede Buisman model in this way that Buisman model simulate settlement due to secondary consolidation of clay in proportion with logarithm of time.

But classical modelling has not proved to be always necessary and many clays behavior can be modelled accurately enough with PLAXIS Soft-Soil-Creep model. Anyway results got from PLAXIS simulation should be considered in hindsight. The different assumptions and the scale of the sample simulated could also influence the results, when applied to bigger scale problems.

Study about getting parameters from the test the most properly has also proved interest. However the first point to consider is using a fitted model, the accuracy and cares about objective acquiring of parameters should only then be regarded. On this point no particular method could be advisable but those that seems first to be correct according to the observer. That’s why, it should be advised to set parameters the values of which
are not that influenced by the way to work them out and make vary, in the assessed range, one parameter after another to chock the model to the actual behavior. Trying to put in practise the different theories and assumptions formerly enunciated (e.g. Mesri) should be considered in the second instance and cautiously.

It could have been interesting to regard how temperature influences the results as it should play a role of importance in Finland. A study about the scale effect and under which conditions parameters could be considered as correct at larger scale, in the construction site, could have also brought useful information.
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PLAXIS version 8, Material models manual.


APPENDIX 1 (additional theoretical consideration)

The relationship between effective stress, strain and strain rate

In 1985 Leroueil et al. conducted a comprehensive study of different tests on various types of clays with the objective of determining the rheological behavior of soft clays. They proposed that the rheological behavior of one-dimensional consolidation of clays is controlled by a unique relationship between stress, strain and strain rate ($\sigma' - \varepsilon - \dot{\varepsilon}$). This relationship can be described by just two functions. The first gives the relationship between preconsolidation pressure and the strain rate, equation (1'). The second relationship described the normalized effective stress-strain curve by means of equation (2'), see Figure 1:

$$\sigma_p' = f(\varepsilon, \dot{\varepsilon})$$  \hspace{1cm} (1')

$$\frac{\sigma_v'}{\sigma_p'} = g(\varepsilon)$$  \hspace{1cm} (2')

where
- $\sigma_p'$ = consolidation pressure
- $\sigma_v'$ = vertical effective stress [kPa]
- $\varepsilon$ = vertical strain
- $\dot{\varepsilon}$ = vertical strain rate [1/s]

$f(\varepsilon, \dot{\varepsilon})$ = a function of vertical strain rate
$g(\varepsilon)$ = a function of vertical strain

The rheological model is in line with the model including sets of isotaches proposed by Suklje (1957).
Figure 1’ Suggested model for natural clays (Leroueil et al., 1985)

The observation that the preconsolidation pressure is dependent on the strain rate has been recognized by many researchers, e.g. Sällfors (1975), Larsson (1981), Graham et al. (1983) and Leroueil et al. (1985) to mention but a few. This behavior can be exemplified by CRS-tests with different strain rates.

In Figure 2’ another important test result (Mesri et al. 1995) is presented, which confirms the behavior described. For a 500mm long sample the effective stress – strain curves of four different sub-layers were monitored. The stress-strain curves vary, depending on the distance of each sub-element to the drainage boundary. For sub-element 1, close the drainage surface, the strain rate is higher than in other sub-elements. The resulting effect is that, for a higher strain rate, a higher magnitude of effective stress was obtained in the initial branch of the curve, i.e. the apparent preconsolidation pressure increased. Analogous results were also reported by Berre and Iversen (1972). Moreover, the results presented in Figure 2.9 show clearly how the consolidation process and the apparent preconsolidation pressure vary in the clay strata due to different drainage conditions.
It can also be noted that the point of EOP, in Fig 2', seems to be equal of all sub-elements. Mesri and Choi (1985) proposed that there is a unique EOP $e$- $\log\sigma'$ curve for any soft clay. This statement is not in line with e.g. Suklje (1957), Berre and Iversen (1972) and Yin and Graham (1996), who concluded that the relationship between strain and effective stress at the EOP depends on the thickness of the clay specimen/layer.

Figure 2’ Consolidation of St-Hilaire clay for pressure increment from 97 to 138 kPa (results from Mesri and al. (1995), reinterpreted and presented by Leroueil and Marques, 1996). $C_\alpha$, secondary compression index; $C_c$ compression index; $\dot{e}$ rate of void ratio and $m' = C_c / C_\alpha$.

In 2001 Leroueil and Kim proposed a non-linear viscoplastic model for one-dimensional consolidation, where the strain is divided into two parts: elastic strains and the viscoplastic strains. This model is a further development of the model presented by Leroueil and al. (1985).
The effect of temperature on the compressibility

The behavior of natural clay during consolidation is evidently not influenced only by the strain rate. Temperature is also an important factor, especially in the normally consolidated range and also in terms of the magnitude of the preconsolidation pressure. The influence of temperature on the compressibility of natural clays has been investigated by authors such as for example Sällfors (1989) and Boudali and al. (1994). In 1994, Boudali and al. proposed a generalization of the model suggested by Leroueil (1985), which takes the temperature into consideration.

Tidfors and Sällfors (1989) found that if the temperature increased from about +7°C, which is the normal temperature in-situ, to about 20°C, the preconsolidation pressure for a high plastic clay decreases with 6 to 10%. Leroueil and Marques (1996) obtained results that were in agreement with that.

However, the temperature in a clay deposit is normally constant and the temperature effects can be neglected in this work.

Determination of the creep parameter from CRS tests

Länsivaara (1995, 1999) proposed a model that made it possible to determine the creep parameter *time resistance number*, $r_s$, from CRS tests with different strain rates. However the model assumed that the compression modulus increases linearly with effective stress. For Swedish clays the compression modulus is evaluated as constant from $\sigma'_c$ to $\sigma'_L$. This implies that the relation becomes more complex and thus more difficult to solve. Länsivaara utilized the unique relation between preconsolidation pressure and effective stress at a given strain (see equations (1') and (2')) and derived:

$$\frac{\sigma'_{cv1}}{\sigma'_{cv2}} = \frac{\sigma'_{v1}}{\sigma'_{v2}}$$

(3')

Where

$\sigma'_{v1} =$ the effective strain for the strain rate $\varepsilon_1$

$\sigma'_{cv1} =$ The preconsolidation pressure for the strain rate $\varepsilon_1$
\[ \sigma'_{v1} = \text{effective stress for the strain rate } \dot{\varepsilon}_1 \]

\[ \sigma'_{cv1} = \text{the preconsolidation pressure for the strain rate } \dot{\varepsilon}_1 \]

In addition to the strain rate relation the equation can be expressed as (Länsivaara 1995):

\[ \frac{\sigma'_{v1}}{\sigma'_{v2}} = \frac{\sigma'_{cv1}}{\sigma'_{cv2}} = \left( \frac{\dot{\varepsilon}_1}{\dot{\varepsilon}_2} \right)^B \tag{4'} \]

Where the parameter B was determined. Länsivaara proposed that parameter B is equal to equation (2.19), i.e.

\[ B = \frac{m}{r_s} = \frac{C_a}{C_c} \tag{5'} \]

Which describe the relation between the creep and primary compression parameters in the equation.

Hence the time resistance number can be determined from:

\[ r_s = \frac{M(\sigma')}{\sigma'.B} \tag{6'} \]

Länsivaara (1999) found that the value of B for Finnish clays is about 0.073.

Leroueil and Kim (2001) suggested an elastic viscoplastic (EVP) model. The model utilizes the relationship between the preconsolidation pressure and strain rate to describe the viscous behavior. By conducting CRS tests with different strain rates, determining the preconsolidation pressure at each strain rate and then plotting the results in a diagram as shown in Figure 3', thus making it possible to interpret a linear relationship between the plotted results. The equation describing the relation between
preconsolidation pressure and viscoplastic strain rate, \( \sigma'_p = f(\dot{\varepsilon}_v^{vp}) \), can be expressed as a linear function in a \( \log \sigma'_p = \log \dot{\varepsilon}_v^{vp} \) diagram:

\[
\log \sigma'_p = \Gamma + C_p \log \dot{\varepsilon}_v^{vp}
\]  

(7')

Where \( \Gamma = \) the value of \( \log \sigma'_p \) at \( \dot{\varepsilon}_v^{vp} = 10^0 \) 1/s

\( \varepsilon_v^{vp} = \) viscoplastic strain rate

\[
C_p = \left( \frac{\partial \log \sigma'_p}{\partial \log \varepsilon_v^{vp}} \right)_{\varepsilon_v^{vp} = 10^0}
\]

the preconsolidation index is denoted \( C_p \) and is equal to the value of \( C_\alpha / C_c \) which according to Mesri and Castro (1987) is between 0.03-0.05.

\[10^{-9} 10^{-8} 10^{-7} 10^0 \log \dot{\varepsilon}_v^{vp}\]

\( \Gamma \)

\( C_p \)

\[\log \sigma'_p\]

**Figure 3’** \( \text{Definition of the parameter } C_p \text{ and } \Gamma \) (Kim and Leroueil, 2001)

These two parameters define the viscous behavior of the clay.
Sampling

In order to carry out the tests, clay samples are taken from different sites in Finland. Here are some:

![Map showing sampling sites](image)

I have attended a course explaining in situ how to extract an undisturbed sample. The method consists in a first part of analysing the soil in place to know approximately the depth and thickness of the different layers. Then as we were interested in clay, a sample of this kind of soil at the chosen depth was extracted with the help of a standard piston sampler. To get the less disturbed sample as possible, avoiding vibrations is fundamental and hammer hits must be used as the worst solution. Here the stiffness of the soil was soft enough not to use predrilling. The sample was thus preserved in the piston sampler until its use in the laboratory.
Classification data

Criteria for distinguishing soils are not necessarily the same for different classification systems. Soil texture is a good example of the problems involved in correlating classifications between two or more systems. Texture describes the proportion of different size classes of the mineral part of the soil. For the same soil, texture-class names can differ depending on the classification system used. Even if the names are the same, the limits often differ.
The problem continues with particle-size classes. For example, clay is defined as <0.002 mm in diameter by some systems and <0.005 mm by others. Other physical, chemical, and biological characteristics have similar discrepancies between systems which makes one to one correlation between systems nearly impossible unless a detailed soil description is available.

The Finnish classification system is particular for the reason it depends on numerous parameter. We have to know in order to classify a Finnish soil: The organic content, the liquid limit, percentage of the different grain’s size contained and the geological history of the site where the sample comes from.

The tests used in the laboratory to get these characteristics are:

- Organic content (800°C heating)
- Liquid limit: fall cone test, Casagrande test. (see appendix 2 below)
- Percentage of the different grain’s size: densimeter test.

Even if the methods and the limits differ from a classification to another the characteristics considered to determine the class of the soil are the same e.g. the unified soil classification.

<table>
<thead>
<tr>
<th>First and/or second letters</th>
<th>Definition</th>
<th>Second letter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>G</td>
<td>gravel</td>
<td>P</td>
<td>Poorly graded (well sorted)</td>
</tr>
<tr>
<td>S</td>
<td>Sand</td>
<td>W</td>
<td>well graded (poorly sorted)</td>
</tr>
<tr>
<td>M</td>
<td>Silt</td>
<td>H</td>
<td>High plasticity</td>
</tr>
<tr>
<td>C</td>
<td>clay</td>
<td>L</td>
<td>Low plasticity</td>
</tr>
<tr>
<td>O</td>
<td>Organic</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 1" The unified soil classification

<table>
<thead>
<tr>
<th>Major divisions</th>
<th>Group symbols</th>
<th>Group name</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coarse grained soils</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sand more than 50% retained on No.200 sieve</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gravel &gt; 50% of coarse fraction retained on No.4 sieve</td>
<td>GW</td>
<td>well-graded gravel, fine to coarse gravel</td>
</tr>
<tr>
<td>Gravel with fines</td>
<td>GP</td>
<td>poorly-graded gravel</td>
</tr>
<tr>
<td>Sand ≥ 50% of coarse fraction passes No.4 sieve</td>
<td>SW</td>
<td>well-graded sand, fine to coarse sand</td>
</tr>
<tr>
<td>Sand with fines</td>
<td>SP</td>
<td>poorly-graded sand</td>
</tr>
<tr>
<td>Fine grained soils</td>
<td></td>
<td></td>
</tr>
<tr>
<td>silt and clay liquid limit &lt; 50</td>
<td>ML</td>
<td>Silt</td>
</tr>
<tr>
<td>Organic</td>
<td>CL</td>
<td>Clay</td>
</tr>
<tr>
<td>silt and clay liquid limit ≥ 50</td>
<td>Inorganic</td>
<td></td>
</tr>
<tr>
<td>MH</td>
<td>organic clay, organic silt</td>
<td></td>
</tr>
<tr>
<td>OH</td>
<td>organic clay, organic silt</td>
<td></td>
</tr>
<tr>
<td>Highly organic soils</td>
<td>PT</td>
<td>Peat</td>
</tr>
</tbody>
</table>

Other tests

Fall cone test

Operating method

A slice of the sample is cut and put under a loaded cone. The gauge is set to zero and the cone is brought just upon the surface of the sample. The principle is then to let the loaded cone fallen and to check the value of the cone driving in, on the gauge.
NB: the load applied depends on the estimated undrained shear strength forces of the sample.

![Fall cone test apparatus](image)

**Results processing**

The penetration value can be now converted into a value for undrained shear strength force thanks to tables. We get thus a value of undrained shear strength force as an estimation confirmed later by the unconfined compression stress. The results are often higher for this test than for the unconfined compression test but it’s a good means to certify the results.

The penetration value can also be converted to assess the liquid limit of the sample, indeed the Casagrande apparatus is nowadays only used to verify the value obtained. The reason of this is the disparate results got with this test.

We can note that the sensitivity of a sample can also be estimated with this test. To assess this characteristic we proceed the same way but on a remoulded sample and we compare the value with the one obtained with an undisturbed sample.
Unconfined compression test

*Operating method*

The goal of this test is also to get the undrained shear strength value. A sample from the piston sampler is put under a load. The borders of the sample are let free to move. The load is set by applying a constant strain rate on the sample until the failure. During this test the load applied and the settlements of the samples are checked.

*Results processing*

To process the data we plot the load-displacement curve. Thus we can determinate the undrained shear strength of the soil and compare it to the one obtained with the Fall cone test.
APPENDIX 3

Taasia 21D1

Parameters:

- Dimensions of the sample:
  - $H_{\text{init}} = 20$ mm
  - $A = 2000$ mm$^2$

- $\sigma_1 = \sigma$ applied = 200 kPa
- $\sigma_{10} = \sigma$ applied at the previous load step = 100 kPa
- $h_0 = \text{height of the sample at the end of the previous load step} = 19,172$ mm

- $\lambda^* = 0,256$
- $\kappa^* = 7,81,\text{E}-3$ ($\lambda/\kappa = 32,7$)
- $\mu^* = 5,348,\text{E}-3$
- $k = 5,\text{E}-6$ m/day
- $e_0 = 2,7$
- $POP = |\sigma_p - \sigma_{yy}^0| = |90 - 0| = 90kPa$

- $c = 2$ kPa
- $\varphi = 24^\circ$
- $\psi = 0^\circ$

- $\gamma_{\text{sat}} = 14,6$ kN/m$^3$
- $\gamma_{\text{unsat}} = 7,3$ kN/m$^3$
Oedometer test: Taasia 21D1

Figure 1’’’ Computed/observed settlement of the 21 oedometer test’s sample

Error at 70 days [%]: 3.9

**Taasia 26B1**

Parameters:

- Dimensions of the sample:
  - $H_{init} = 20$ mm
  - $A = 2000$ mm$^2$

- $\sigma_1 = \sigma$ applied = 200 kPa
- $\sigma_{10} = \sigma$ applied at the previous load step = 100 kPa
- $h_0 = \text{height of the sample at the end of the previous load step} = 18,757$ mm

- $\lambda^* = 2,031.E-1$
- $\kappa^* = 2,381.E-2$
- $\mu^* = 5,25.E-3$
- $k = 4.E-6$ m/day
• $e_0 = 2.52$
• $POP = |\sigma_p - \sigma_{yy}^0| = |100 - 0| = 100kPa$

• $c = 2 \text{kPa}$
• $\varphi = 24^\circ$
• $\psi = 0^\circ$

• $\gamma_{sat} = 14.77 \text{kN/m}^3$
• $\gamma_{unsat} = 7.64 \text{kN/m}^3$

![Oedometer test: Taasia 26B1](image.png)

Figure 2''' Computed/observed settlement of the 26 oedometer test's sample

Error at 70 days [%]: 4.3
**Vanttila 4452**

Parameters:

- **Dimensions of the sample:**
  - $H_{\text{init}} = 15$ mm
  - $A = 1380$ mm$^2$

- $\sigma_1 = \sigma$ applied $= 42,4$ kPa
- $\sigma_{10} = \sigma$ applied at the previous load step $= 21,4$ kPa
- $h_0 = \text{height of the sample at the end of the previous load step} = 13,606$ mm

- $\lambda^* = 2,214.E-1$
- $\kappa^* = 5,714.E-3$
- $\mu^* = 7,687.E-3$
- $k = 3,119.E-5$ m/day
- $\varepsilon_0 = 3,17$
- $\text{POP} = |\sigma_p - \sigma_{yy}^0| = |13 - 0| = 13kPa$

- $c = 2$ kPa
- $\varphi = 24^\circ$
- $\psi = 0^\circ$

- $\gamma_{\text{sat}} = 13,56$ kN/m$^3$
- $\gamma_{\text{unsat}} = 6,36$ kN/m$^3$
Figure 3: Computed/observed settlement of the 4452 oedometer test's sample

Figure 4: Computed/observed strain of the 4452 oedometer test's sample

Error at 68 days [%]: 2.9
Vanttila 4453

Parameters:

- **Dimensions of the sample:**
  - $H_{\text{init}} = 15$ mm
  - $A = 1380$ mm$^2$

- $\sigma_1 = \sigma$ applied = 42.8 kPa
- $\sigma_{10} = \sigma$ applied at the previous load step = 21.4 kPa
- $h_0$ = height of the sample at the end of the previous load step = 14.352 mm

- $\lambda^* = 1.683 \times 10^{-1}$
- $\kappa^* = 1.359 \times 10^{-2}$
- $\mu^* = 1.077 \times 10^{-2}$
- $k = 1.607 \times 10^{-5}$ m/day
- $e_0 = 3.037$
- $\sigma = 3.037 \times 10^{-2}$

- $POP = \left| \sigma_p - \sigma_{yy}^{10} \right| = 25 - 0 = 25$ kPa

- $c = 2$ kPa
- $\varphi = 24^\circ$
- $\psi = 0^\circ$

- $\gamma_{sat} = 14.12$ kN/m$^3$
- $\gamma_{unsat} = 6.62$ kN/m$^3$
Figure 5”” Computed/observed settlement of the 4453 oedometer test’s sample

Figure 6”” Computed/observed strain of the 4453 oedometer test’s sample

Table 1”” Vanttila 4453, Final error

<table>
<thead>
<tr>
<th>Preconsolidation pressure - σp</th>
<th>Error [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>21,2</td>
</tr>
<tr>
<td>20</td>
<td>5,1</td>
</tr>
</tbody>
</table>
**Perno 116**

Parameters:

- **Dimensions of the sample:**
  - \( H_{\text{init}} = 19 \text{ mm} \)
  - \( A = 4570 \text{ mm}^2 \)

- \( \sigma_1 = \sigma \text{ applied} = 12.5 \text{ kPa} \)
- \( \sigma_{10} = \sigma \text{ applied at the previous load step} = 6.25 \text{ kPa} \)
- \( h_0 = \text{height of the sample at the end of the previous load step} = 17.60 \text{ mm} \)

- \( \lambda^* = 1.218 \times 10^{-1} \)
- \( \kappa^* = 1.812 \times 10^{-2} \)
- \( \mu^* = 1.0857 \times 10^{-2} \)
- \( k = 7.4649 \times 10^{-5} \text{ m/day} \)
- \( e_0 = 5.6 \)
- \( POP = |\sigma_p - \sigma_{yy}| = |6 - 0| = 6 \text{kPa} \)

- \( c = 2 \text{ kPa} \)
- \( \varphi = 24^\circ \)
- \( \psi = 0^\circ \)

- \( \gamma_{\text{sat}} = 12.58 \text{ kN/m}^3 \)
- \( \gamma_{\text{unsat}} = 4.09 \text{ kN/m}^3 \)
**Oedometer test: Perno 116**

*Figure 7""*  Computed/observed settlement of the 116 oedometer test’s sample

*Figure 8""*  Computed/observed strain of the 116 oedometer test’s sample

**Table 2""**  Perno 116, sigma1 = 12.5kPa, Final error

<table>
<thead>
<tr>
<th>Preconsolidation pressure - $\sigma_p$</th>
<th>Error at 10 days [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>20</td>
</tr>
<tr>
<td>6</td>
<td>29</td>
</tr>
</tbody>
</table>


**Suurpelto 4532**

Parameters:

- **Dimensions of the sample:**
  - \( H_{\text{init}} = 15 \text{ mm} \)
  - \( A = 1590 \text{ mm}^2 \)

- \( \sigma_1 = \sigma \text{ applied} = 25 \text{ kPa} \)

- \( \sigma_{10} = \sigma \text{ applied at the previous load step} = 12.5 \text{ kPa} \)

- \( h_0 = \text{height of the sample at the end of the previous load step} = 14.11 \text{ mm} \)

- \( \lambda^* = 1.4858.\text{E-1} \)

- \( \kappa^* = 7.1668.\text{E-3} \)

- \( \mu^* = 1.239.\text{E-2} \)

- \( k = 1.4688.\text{E-5} \text{ m/day} \)

- \( \epsilon_0 = 4.665 \)

- \( POP = |\sigma_p - \sigma_{yy}^0| = |9 - 0| = 9kPa \)

- \( c = 2 \text{ kPa} \)

- \( \varphi = 24^\circ \)

- \( \psi = 0^\circ \)

- \( \gamma_{\text{sat}} = 12.84 \text{ kN/m}^3 \)

- \( \gamma_{\text{unsat}} = 4.45 \text{ kN/m}^3 \)

For this test the value of \( C_{\alpha} \) used is the one obtained directly from experimentation as modelling the behavior during secondary compression (varying with the stress) has not been possible. \( C_{\alpha} = 2.85\% \).
Figure 11”” Computed/observed settlement of the 4532 oedometer test’s sample

Figure 12”” Computed/observed strain of the 4532 oedometer test’s sample

Error at 231 days [%]: 22.4
**Suurpelto 4533**

Parameters:

- **Dimensions of the sample:**
  - $H_{\text{init}} = 15 \text{ mm}$
  - $A = 1590 \text{ mm}^2$

- $\sigma_1 = \sigma_{\text{applied}} = 25 \text{ kPa}$
- $\sigma_{10} = \sigma_{\text{applied at the previous load step}} = 12.5 \text{ kPa}$
- $h_0 = \text{height of the sample at the end of the previous load step} = 14.588 \text{ mm}$

- $\lambda^* = 1.339 \times 10^{-1}$
- $\kappa^* = 1.879 \times 10^{-2}$
- $\mu^* = 5.739 \times 10^{-3}$
- $k = 9.063 \times 10^{-6} \text{ m/day}$
- $e_0 = 2.846$
- $POP = |\sigma_p - \sigma_{yy}^0| = |20 - 0| = 20 \text{kPa}$

- $c = 2 \text{ kPa}$
- $\varphi = 24^\circ$
- $\psi = 0^\circ$

- $\gamma_{\text{sat}} = 13.89 \text{ kN/m}^3$
- $\gamma_{\text{unsat}} = 6.43 \text{ kN/m}^3$
One can notice a huge difference between the model and what is actually observed this is due to the strange behavior of this clay and how we have modelled it. Indeed the primary consolidation occurs very late so the first modelling line of the Casagrande’s construction is very steep. (c.f plot below Casagrande’s construction)
Figure 15’’’ Computed/observed strain of the 4533 oedometer test’s sample