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Optimizing Programming by Demonstration for in-contact task models by Incremental Learning

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Preface

First of all, I would like to thank my supervisor Ville Kyrki and my instructor Alberto Montebelli for giving me the chance to work on this project. I want to thank Ville especially for always being on hand with help and advice and giving me free choice of the topic and direction of the thesis. My deepest gratitude goes to Alberto for his guidance, motivation and confidence he placed in me all through the work and his assistance to improve the language and style of this thesis.

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Despite the increasing usage of robots for industrial applications, many aspects prevent robots from being used in daily life. One of these aspects is that extensive knowledge in programming a robot is necessary to make the robot achieve a desired task. Conventional robot programming is complex, time consuming and expensive, as every aspect of a task has to be considered. Novel intuitive and easy to use methods to program robots are necessary to facilitate the usage in daily life.

This thesis proposes an approach that allows a novice user to program a robot by demonstration and provides assistance to incrementally refine the trained skill. The user utilizes kinesthetic teaching to provide an initial demonstration to the robot. Based on the information extracted from this demonstration the robot starts executing the demonstrated task. The assistance system allows the user to train the robot during the execution and thus refine the model of the task.

Experiments with a KUKA LWR4+ industrial robot evaluate the performance of the assistance system and advantages over unassisted approaches. Furthermore a user study is performed to evaluate the interaction between a novice user and robot.

**Keywords:** Programming by Demonstration, Incremental Learning, Human-Robot Interaction, Assistance
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<td>Bayesian Information Criterion</td>
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<td>Dynamic Movement Primitives</td>
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<td>DOF</td>
<td>Degree of Freedom</td>
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<td>FRI</td>
<td>Fast Research Interface</td>
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<td>Programming by Demonstration</td>
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<td>User Datagram Protocol</td>
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Chapter 1

Introduction

Robots are increasingly utilized in industrial and domestic applications [IFR, 2014]. However, several challenges avert them from being extensively used in daily life. For example, safety regulations well summarize current concerns regarding humans sharing a common workspace with robots. In human-robot interaction, conveying the intention of a user to the robot constitutes another open problem. Crucially, the high costs for robot programming are a further issue to be addressed, as applying conventional programming to state of the art applications is complex, time consuming and expensive. In fact, every aspect of a potentially complex task has to be explicitly considered, and such an assessment is often not simple or even feasible.

Programming by Demonstration (PbD) has developed to constitute a wide field within robotics [Billard et al., 2008]. PbD has introduced novel ways to address aforementioned challenges thus facilitating the use of robots in daily life. Once the general software infrastructure for PbD is available, robots can be trained on new tasks and become operative within minutes. Accordingly, the traditional role of the programmer as the person who implements code is overtaken by an instructor, who directly provides demonstrations of the required skill to the robot. The goal of PbD is to enable the robot to extract necessary and important information about the task from the demonstration and generalize over one or several demonstrations to novel situations. In contrast to conventional programming, where trajectories are programmed by an expert and then replayed, the robot can be directly instructed by a person without any prior knowledge in robotics. Therefore, new possibilities for Human Robot
Interaction (HRI) and the integration of robots in human workspaces to solve collaborative tasks arise. Calinon et al. [2014] described the current situation in robotics as “reminiscent of the pre personal-computer age when people needed to be expert in computer programming to make the computer achieve a desired task. As with personal computers, the development of robots and the reduction of cost are now reaching a point where more natural and user-friendly interfaces are required to re-program the robot”.

Tasks for industrial robots normally require a physical interaction between the robot and an object, and are thus called in-contact tasks. Often, such interactions require a precise control of the arising interaction forces, as too low or too high forces might result in a failure of the task or even damage the robot or its environment. The interaction forces that can cause undesired effects are not only the forces exerted by the robot, but include friction or external forces. Friction, for example, can cause the manipulator to jerk or bounce. These aspects increase the complexity of programming a robot in an industrial setting even further, as all possible interactions of the robot with its environment have to be considered and reasonable constraints have to be implemented to protect the robot and its environment while ensuring the fulfillment of the task. This complexity can be reduced by PbD, as the instructor can perceive the results of the exerted forces and act accordingly during the demonstration.

In a near future, small and medium size companies will have an increasing interest in industrial robots as Industry 4.0, the combination of factories with virtual reality, plays a growing role in manufacturing [IFR, 2014]. Energy-efficiency, growing consumer markets, decreasing products’ life cycles and an increase in the variety of products are only a few reasons for increasing automation and demand for industrial robots and their quick and flexible programming. In fact, orders of goods produced in low quantity could be optimally processed by flexibly training a robot by demonstration without necessarily hiring a software engineer.

Current PbD approaches have proven successful in teaching robots relatively complex tasks which would require extensive and expensive software development by expert programmers. However, PbD also presents several open issues. A basic issue, called correspondence problem, occurs due to different embodiment between the instructor and robot [Calinon and Billard, 2007]. A further
1.1 Problem

Problem relates to the quality of the demonstration. Through the demonstration, the instructor has to effectively transfer to the robot the dynamics required by the task. Several teaching methods will be presented in Section 2.1. All these methods force the instructor to face unfamiliar conditions during the demonstration of the task. For example, they might require additional sensors attached to his body or dragging a robotic manipulator attached to the familiar tool. Such requirements can negatively affect the quality of the demonstration. Poor demonstrations will result in poor skills acquired by the robot. Thus, it is necessary to support the human instructor with natural and intuitive means to effectively convey skills to the robot. In principle, a robotic system can improve the quality of the demonstration and rise above the level of skill that had initially been demonstrated. Such refinement techniques can contribute to such a natural and intuitive training interface and are the focus of this thesis.

1.1 Problem

Little research is currently available in the technical literature for PbD robot training for in-contact tasks, despite their significance for the industry. Also, the use of state-of-the-art industrial robots with in-built force and joint torque sensors and variable compliance for in-contact tasks relies on relatively limited research. Traditional industrial robots have to work in controlled production lines, where the poses of tools and work pieces are strictly known and their environment is completely predictable. The compliance offered by state-of-the-art robots ensures a good contact between tool and work piece, even if the poses of both slightly differ from the nominal poses. Furthermore, compliant manipulators are safer, as uncontrolled high forces between tool and work piece are prevented.

Therefore, this new class of robots, like the KUKA LWR [Bischoff et al., 2010], are particularly well suited for in-contact tasks. The KUKA LWR has furthermore the advantage of torque sensors in every joint and a force torque sensor in its wrist. Thus no additional hardware is required to measure forces exerted by the robot or external forces that act upon the robot. Montebelli et al. [2015] developed a system that encoded simultaneously the trajectory of the tool and the force profile of a task. The system was tested by teaching a KUKA
LWR4+ robotic arm to plane a wooden plank. The same control system was further extended to handle disturbances in dynamic environments during the reproduction of a sequence of hand written characters [Steinmetz et al., 2015].

The general problem of PbD is to transfer the professional skill of an instructor to a robot, while preserving the quality of the skill. The work reported in this thesis aims to the creation of a human-robot interface that feels natural, intuitive and user friendly to the human instructor in order to effectively transfer skills for physical in-contact tasks to a robot. The experiments reported in the thesis contribute to its goal by introducing and demonstrating the coordinated use of two main elements of such an interface: Incremental Learning (IL) and Proactive Assistance (PA). As training progresses through a sequence of multiple demonstrations, the system can build up confidence about its knowledge of the task (IL). As such a confidence is built, the robot will reduce its compliance and actively make use of the accumulated information to assist the movements of its instructor. Furthermore is the force of the human exerted on the robot measured and amplified (PA), thus the effective inertia of the robot attached to the tool is reduced. This interface has the ambition to ensure minimal disturbance to the instructor by minimizing the impact of unfamiliar modifications of the tool and procedures for the execution of the task.

Therefore the approach presented by Montebelli et al. [2015] will be extended firstly, by implementing the possibility to update the model of the system incrementally. Secondly, virtual tool dynamics will be implemented, which will reduce the inertia of the robot by amplifying the force exerted by the instructor.

1.2 Structure

This thesis is structured in six chapters. Chapter 2 will offer an overview of PbD and training methods in use. Chapter 3 will present current research of machine learning techniques, used to refine the quality of reproduction after initial demonstrations. Chapter 4 will present the hardware and software used in this thesis to support the experimental work. Experiments and results are presented in Chapter 5. Chapter 6 contains a critical discussion and associated conclusions.
Chapter 2

Programming by Demonstration

This chapter offers an overview of how demonstration and reproduction works in PbD. First, different teaching methods will be introduced. The two main classes of methods used in the technical literature, symbolic and trajectory-based learning, are presented in detail.

2.1 Training Methods

In PbD, transferring a physical skill from a human to a robot is done by demonstrations. Several methods exist to demonstrate a skill to a robot, which can be categorized into teleoperation, kinesthetic teaching and observational learning [Kormushev et al., 2013].

Teleoperation is a technique, where the robot is remotely controlled by the instructor with an input device, like a joystick or haptic gloves. Teleoperating an overactuated robot, which has more than 6 DOF, is complicated, especially if smooth and dexterous motions are desired. Teleoperation is used, among others, for teaching grasping tasks, as done by Schmidts et al. [2011], who used a haptic glove to record both force and position data. The combination of both data led to higher success rates in teaching grasping movements and an improved generalization capability.

In kinesthetic teaching, the robot is grabbed and moved manually by the instructor and the movements are recorded. However, the robot needs to be small
and lightweight with a gravity-compensation controller to be effectively moved manually by a human instructor. Furthermore it can be difficult with complex robots to only move desired limbs, without moving other parts of the robot too. The aim of this thesis is to implement a system that provides assistance during kinesthetic demonstrations and reduces the complexity of kinesthetic teaching. An advantage is that kinesthetic teaching can be used to directly teach relatively complex in-contact tasks, for example wood planing as in [Montebelli et al., 2015].

Observational learning methods make use of sensors, which can be external or attached to the instructor, to perceive the actions of the instructor. These sensors can be RGBD-cameras or motion sensors worn by the instructor. Observational learning offers a teaching process which is easy and natural for the instructor and it is possible to generate very smooth and human-like motions from such teaching trials. Calinon and Billard [2007] used a combination of observational learning, with motion sensors, and kinesthetic teaching to teach smooth trajectories and then improve them by manually moving the limbs of the robot to reduce the impact of the correspondence problem.

One issue in PbD is to find a mapping between the body of the instructor and the robot that suits the execution of the task. An advantage of teleoperation and kinesthetic teaching over observational teaching is, that the robot can perceive all actions with its own sensors, eluding mapping problems between instructor and robot. Conversely, in observational learning, all actions are perceived by external sensors and thus have to be mapped to the robot.

### 2.2 Representing Actions

Skills can be learned in two different ways: At a more abstract level, skills can be interpreted as a concatenation of several primitive actions, each represented by a symbol. Learning on this level is called *symbolic learning*. An alternative is to represent skills at trajectory level, which is called *trajectory learning*.
2.2 Representing Actions

2.2.1 Symbolic Learning

The principle of symbolic learning is that basic actions, identified with symbols, are defined beforehand and a demonstration is encoded as a sequence of these symbols. Symbolic learning consists of several steps, that can be seen in Figure 2.1.

![Symbolic Learning Diagram](https://example.com/symbolic-learning-diagram.png)

Figure 2.1: Principle of Symbolic Learning (Adapted from [Ekvall and Kragic, 2006])

Ekvall and Kragic [2006] described the principles of symbolic learning. First one or multiple demonstrations are given and perceived by the system. In the segmentation step, machine learning techniques, for example Hidden Markov Models (HMM) are used to partition the demonstration into a set of primitives. Typically, to allow the recognition of primitives, they have to be defined in advance. In the state generation block all given demonstrations are used to model subtasks as states. These states are used for generalization in the task generalization block. From the demonstrations constraints are extracted, which need to be fulfilled to execute the task properly. An example of such constraints could be to first open a bottle before pouring its content in a glass. Figure 2.2 shows how constraints are learned from demonstrations. In both demonstrations, state B comes before the states F and G. Thus it is a constraint that B has to be executed before F or G. With more demonstrations, more constraints can be learned. With both, the states and constraints, possible execution sequences are build up. If only one demonstration is provided, the system will execute the states in the same order as demonstrated.
2.2 Representing Actions

The execution sequence is calculated in the *planning block*, where the environment is taken into account. The execution is planned in a way that the goal can be reached, for example by defining how to grab an object or by avoiding collisions given the current context. Then the sequence is executed. If the goal is not reached, the next sequence is planned until the goal is reached.

Symbolic learning enables a robot to learn whole tasks as a sequence of abstract high-level states. Thus it is easier for human users to understand what the robot is doing and why. The disadvantage of this approach is the huge amount of prior knowledge that has to be provided for example action primitives and properties of the objects in the workspace.

2.2.2 Trajectory Learning

In trajectory learning trajectories are learned from provided demonstrations with the goal to generalize over these demonstrations and generate trajectories fulfilling the requirements of the demonstrated task. These trajectories can be represented as probability distributions or dynamic models. It is necessary to choose a space in which the robot will operate, depending on the task. Trajectories can be recorded in joint space, task space or torque space [Billard et al., 2008]. For executing a task, it might be also necessary to record additional data. For example, in-contact tasks usually require the integration of positional information with information about exerted forces [Kormushev et al., 2011, Montebelli et al., 2015, Steinmetz et al., 2015].
2.2 Representing Actions

Trajectory encoding with Statistical Models

One possible approach to encode trajectories is to use statistical models. The hypothesis behind this approach is that although several demonstrations might differ between each other they should be very similar during crucial elements of the task. Therefore, a mean trajectory and its variance can be calculated. In this case, the variance can be interpreted as a measure for how close the reproduced trajectory has to follow the mean trajectory during the execution of the task. Portions of the trajectory characterized by high variance (i.e. less homogeneous behavior), can be exploited for fulfilling additional requirements or, in general, to react to changes in the environment, e.g. obstacle avoidance [Mühlig et al., 2009]. Invariant portions of the trajectory are presumably important to successfully reach a goal. Accordingly, they should closely match the mean trajectory. Alternative methods that have been suggested to model the probability density functions of the demonstrated trajectories are presented in the following sections.

Gaussian Mixture Models

The use of a Gaussian Mixture Model (GMM) consists of two steps: Observation and learning. During the observation phase datapoints are acquired with sensors. The data is then usually preprocessed by temporal normalization. In fact, demonstrations typically present temporal distortions and inconsistencies, as a human will not be able to give multiple identical demonstrations. Therefore, to retrieve useful information from multiple demonstrations, the data has to be temporally normalized. For this purpose Dynamic Time Warping (DTW) is often used, where the trajectories of all demonstrations are aligned to minimize the distance between each of them [Mühlig et al., 2009]. Figure 2.3 shows the effect of using DTW on acquired demonstrations. Only after the application of DTW it is possible to find a reasonable mean and covariance. The learning phase follows the observational phase, where GMM are built with several Gaussians. Each Gaussian consists of a mean vector, a covariance matrix and an initial likelihood, the prior. The model is then created with a mixture of several Gaussians with the dimensionality of the datapoints plus time [Calinon et al., 2007, Mühlig et al., 2009]. To retrieve the parameters (mean, covariance and prior) from the mixture of all Gaussians, different algorithms can be used to train the GMM, such as the expectation-maximization (EM) algorithm. The EM algorithm maximizes the
2.2 Representing Actions

Figure 2.3: GMM without DTW (left) and with DTW (right). The green ellipses show the learned mean and covariances (Source: [Mühlig et al., 2009])

likelihood that the GMM represents the probability density function of the acquired data during the observation phase [Mühlig et al., 2009]. The Bayesian Information Criterion (BIC) is often used to determine the number of Gaussians that produces the best model and to quantify the quality of a model [Mühlig et al., 2009]. To find the best amount of Gaussians components, the number of components is increased, the GMM trained and the quality of the model then evaluated by the BIC. The smallest BIC value refers to the estimated optimal amount [Mühlig et al., 2009]. Retraining the GMM after each step is time consuming, therefore Mühlig et al. [Mühlig et al., 2009] proposed to merely approximate the ideal model, resulting in sufficient accuracy and a speedup of two orders of magnitude compared to using EM for each step.

GMM have the advantage that there is no distinction between inputs and outputs, any subset of the dimensions can be defined as the input, while the remaining subset is defined as the output. This mean in practice that, for example, conditioning on the outputs of a model of the forward dynamics of an robotic arm gives automatically a model of the inverse dynamics of that robotic arm [Cohn et al., 1996].

Locally Weighted Learning  Locally Weighted Learning (LWL) is a class of techniques for the approximation of functions around the current point of interest [Atkeson et al., 1997]. These methods assign a weight to every new data set, specifying the influence of this data on the learning process. This weight is depending on the position of the input points in dataspace relative to
2.2 Representing Actions

the point which has to be predicted. Data points close to the prediction point have higher weights [Friedman, 1995]. In contrast to model-based methods, such as GMM, where training data are generally discarded after every learning trial, LWL methods, which are memory-based, relearn from all data when a prediction is needed. This is a useful feature for IL. One method, called *Locally Weighted Regression* (LWR), implies a regression that is performed locally around the point of interest, as it can be seen in Figure 2.4 [Cohn et al., 1996]. The problem with most LWL methods is, that with an increase of dimensions the number of local models needed for accurate estimations increases exponentially. This is also true for LWR and thus it is not memory efficient and not suited for high-dimensional applications [Vijayakumar et al., 2005]. Vijayakumar et al. [2005] developed another LWL method called *Locally Weighted Projection Regression* (LWPR), which combines LWR and projection regression, which reduces the dimensionality locally. LWPR is specially developed for IL. It provides fast learning and is computationally efficient, as not all training data have to be kept in memory.

![Figure 2.4: Data points are weighted depending on their distance to the point of interest x and a regression is calculated. (Source:[Cohn et al., 1996])](image)

**Hidden Markov Models**  
Hidden Markov Models (HMM) are Bayesian networks, which represent probabilities over a sequence of observations. A HMM consists of states (denoted as 1 and 2), transition probabilities $t$ and the probability $p_j(x)$ for an emitted observation symbol $x$ in state $j$. The states are proba-
bility distributions, defined by mean and covariance matrix. The last parameter of a HMM is the initial probability \( \pi_j \) of being in state \( j \). These parameters can be learned by the EM or Baum-Welch Algorithm or by optimization techniques like the Gradient Descent algorithm [Calinon et al., 2010a][Khreich et al., 2012].

HMMs are defined by two properties: Hidden states and the Markov property. Hidden means, that the emitted symbol sequence is observable, but the actual state within the sequence of states is not. The Markov property described the fact, that the current state is only dependent on the previous state [Ghahramani, 2002]. HMMs are widely used for many different purposes, like speech recognition [Rabiner, 1989], handwritten word recognition [El-Yacoubi et al., 1999] or cybersecurity [Warrender et al., 1999]. Their capability to model real-world phenomena, like human motion, in terms of simple and compact models, makes them interesting for PbD applications [Khreich et al., 2012]. Inamura et al. [Inamura et al., 2004] described in this context the Mimesis Model, which uses HMMs to recognize and generate human motions. Similar to GMM, where the number of Gaussians has to be defined, in HMM the number of states has to be defined. Also for HMM the BIC-criterion can be used to find the needed number of states. A drawback of HMMs is, that a high number of states is needed to correctly reproduce complex motions or a smoothing procedure is used, which reduces important peaks in the motion [Calinon et al., 2010a].

**Trajectory encoding with Dynamical Systems**

Dynamical systems are another possibility for learning skills at the trajectory level. They are designed to be stable and robust against perturbations. In PbD, a widely used model is Dynamic Movement Primitives (DMP)[Schaal et al., 2007].

**Dynamic Movement Primitives** DMPs have received a lot of attention in the robotics community in recent years. This method was introduced 2002 [Ijspeert et al., 2002a,b] and further developed by Schaal et al. [2007]. A detailed overview was presented by Ijspeert et al. [2013]. The principle of DMPs is that a simple and well understood simple attractor system (namely a spring damper system relaxing from an initial to its steady state position) is extended with forcing function terms to remap onto a desired attractor (in the case of
PbD, the demonstrated trajectory). A DMP consists of a canonical and, independently for each demonstration, a transformation system, as it can be seen in Figure 2.5. DMPs were developed to encode both discrete and oscillating trajectories. The canonical system models the behavior of the model equations, e.g. whether it acts as a point attractor or a limit cycle. Furthermore it serves as a replacement of time to make the transformation system formally independent of time [Ijspeert et al., 2013]. The canonical system can be described as

\[ \tau \dot{x} = -\alpha_x x, \]  \hspace{1cm} (2.1)

with a time constant \(\tau\) and a positive constant \(\alpha_x\). \(x\) is a phase variable which converges from an initial state \(x_0\) to zero, where \(x = x_0\) indicates the start and \(x\) close to zero denotes that the goal \(g\) has been reached. The transformation system consists of a simple dynamic system, like a spring-damper system, which is then transformed into a desired attractor system with forcing terms \(f\). Formally:

\[ \tau \dot{z} = \alpha_z (\beta_z (g - y) - z) + f, \]  \hspace{1cm} (2.2)

\[ \tau \dot{y} = z, \]  \hspace{1cm} (2.3)
with positive constants $\alpha_z$ and $\beta_z$, desired position, velocity and acceleration $y, \dot{y}, \ddot{y}$ and forcing term $f$. To let $y$ monotonically converge towards $g$, thus critically damping the system, $\beta_z$ should be defined as $\beta_z = \alpha_z/4$. The forcing term $f$ could be chosen, for example, as

$$f(x) = \frac{\sum_{i=1}^{N} \Psi_i(t) w_i}{\sum_{i=1}^{N} \Psi_i(t)} x(g - y_0),$$

(2.4)

with adjustable weights $w_i$, the initial state $y_0$ and fixed basis functions $\Psi_i$,

$$\Psi_i(x) = \exp \left( -\frac{1}{2\sigma_i^2} (x - c_i)^2 \right),$$

(2.5)

where $\sigma_i$ and $c_i$ are the width and centers of the basis functions [Ijspeert et al., 2013].

To learn the parameters of the system different regression methods can be used, like LWR or LWPR [Ijspeert et al., 2013]. The advantages of DMPs are manifold. It can be used to both classify and replicate movements. Classification can be done with the parameters (weights) of the function approximator. Furthermore it is possible to decompose complex movements into a concatenation of movement primitives [Ijspeert et al., 2013]. DMPs scale well for high dimensionality. Ijspeert et al. [2013] described different methods to cope with multiple DOF. A simple method is to use one canonical system for all DOF and a transformation system for each DOF. One of the main advantages is the possibility of online modification of the primitive. As shown in Figure 2.5, coupling terms are introduced to both the canonical and transformation system. These coupling terms can be used to modify the trajectory online, for example to apply a different scaling [Ijspeert et al., 2013]. Dynamical systems are stable in the presence of small random noise, but for large perturbations, the coupling terms can be used as feedback terms to modify the trajectory accordingly [Billard et al., 2008].

**Comparison**

Despite the differences between described learning methods and the different use cases, almost no comparisons exist in literature. Calinon et al. [Calinon et al., 2010a] compared HMM, LWR, LWPR, DMP and Time-Dependent Gaussian
Mixture Regression (TDGMR), which uses GMM to encode the distribution of spatial and temporal variables, with each other. Five metrics are used in the comparison: Root-Mean-Square (RMS) Error, RMS Error after DTW, Norm of Jerk, learning time and retrieval duration. The RMS error evaluates how accurate in spatial and temporal terms the reproduced trajectory matches the demonstrations. RMS error after DTW emphasizes on the spatial information, as the RMS error is calculated after aligning the trajectories with DTW. The norm of jerk measures the smoothness of a trajectory, based on the derivative of acceleration. As the name implies, the learning time is the time the algorithm needs to learn the trajectory, while the retrieval duration is the computation time of the retrieval process for one iteration. The results for different number of states and seven dimensions can be seen in Figure 2.6. The RMS error before and after DTW shows only a little deviation from the learned trajectory for all examined learning methods. The jerk is smallest with DMP, which generates the smoothest trajectories. The learning time is smallest for DMP and LWR, while HMM and TDGMR, which are both trained with the EM algorithm, show the worst performance. As the EM algorithm used in this test starts its search
procedure randomly, the results are very variable. The online learning capability of LWPR needs special consideration, as ten learning trials with random data has been performed. For a single trial the learning time can be reduced by an order of magnitude. The retrieval time is low for all methods, but for LWR comparatively high with $7 \times 10^{-2}$s, so that it does not appear in the graph anymore. The retrieval time is almost constant for DMP, while it is linearly increasing with the number of states for the other methods. All methods except LWR show a low retrieval time of less than 1 ms and are thus usable for online use.

2.3 Discussion

PbD is an useful approach to teach robots new skills without experts in robotics. Different teaching approaches exist, but kinesthetic teaching proves to be intuitively usable while avoiding the correspondence problem, thus it will be the teaching approach in the process of this thesis. For learning skills two main fields, symbolic and trajectory learning, exist. Symbolic learning requires a great amount of prior knowledge and is thus not as versatile and easy to use as here intended. Trajectory learning offers a great capability of generalization and fast learning. In comparison to other considered methods, DMPs showed little deviation from the demonstrations while producing smooth trajectories with short learning and retrieval time. LWR proved to be the fastest learning method. Thus DMPs will be used to in this thesis, in combination with LWR to learn primitives from demonstrations.
Chapter 3

Post-Training Optimization

The outcome of PbD is a robot with an acquired capability to perform a task. Normally, the quality of its performance is directly related to the quality of the demonstration received by the robot during its training. This chapter will give an overview of methods that address the problem of improving the acquired performance. Two major techniques exist for this improvement. Firstly, following demonstrations, the overall quality can be further enhanced by giving the robot feedback when its execution of the task cannot be considered satisfactory. This feedback can take the form of a new demonstration for the whole task again or can be limited to the unsatisfactory parts of it. Such additional demonstrations are functional to an incremental update of the underlying model. For this reason, this supervised technique is called IL [Cho and Jo, 2013]. Secondly, reward functions can be used to allow the system to automatically explore new behaviors and determine what can be interpreted as beneficial or detrimental behavior. The former will be rewarded whereas the latter will be punished by the reward function. Thanks to the reward function, the robot will explore the states of its environment and the actions to reach them with an unsupervised trial and error method. With the reward function ranking the actions of the robot, the system can balance the exploitation of the already learned actions and the exploration of new solutions to incrementally increase its performance in the given task. This framework is called Reinforcement Learning (RL) [Sutton and Barto, 1998].
3.1 Incremental Learning

Teaching a practical skill in daily life is often done in several steps. First an instructor provides a presentation, then the learner attempts to reproduce, while supervised by the instructor. In case the learner produces a poor reenactment of the task, he or she receives feedback from the instructor about what needs to be improved. Additionally the instructor can show the demonstration again, enabling the learner to generalize over different demonstrations, as it can be seen in Figure 3.1. Such a procedure is designated in robotics as IL [Nicolescu and Mataric, 2003].

![Figure 3.1: Principle of Incremental Learning](Image)

3.1.1 Feedback

The feedback loop shown in Figure 3.1 summarizes the main difference between IL and ordinary PbD approaches. When the replication of the task is unsatisfactory, multiple demonstrations of the whole task (or parts of it) can be performed to incremental update the model. Social cues can be used to highlight situations, for example by pointing or gazing, where the system has to achieve accurate reproduction of crucial details or better performance is required [Calinon and Billard, 2008]. A direct way to offer feedback is by kinesthetic teaching, as described in Section 2.1, where parts of the robot are physically moved. The method of kinesthetic teaching was used with a HOAP-3 robot by Calinon and Billard [2007]. After the initial demonstration, the robot performed the learned skill. The reproduced gestures are then fine-tuned by manually moving the limbs of the robot. The same method was used by Cho and Jo [2013] with a
NAO humanoid robot, with the difference that the robot could withdraw flawed demonstrations (see section 3.1.2).

An interesting research direction addresses the use of pointing and gazing, which attracts the attention of the robot to a certain area or situation to simplify the full potential complexity of conveying the skill. The direction of a human supervisor’s pointing or gazing can be determined with external sensors like stereo cameras. The human instructor will naturally turn his head to the situation which is important for the task. Thus head tracking offers an intuitive way to focus the attention of the robot and to provide useful information. Calinon and Billard [2008] used pointing and gazing information as a prior for the statistical framework, which extracts the task constraints. According to their approach, demonstrated actions received a weighting depending on whether they occurred within the gazing area. The benefit of social cues depends on how accurately the robot can detect what is highlighted. A reliable method to estimate the information in pointing gestures was developed by Park and Lee [2011] to recognize pointing gestures, allowing an exact target selection in 99% of all cases.

A different approach to the problem of creating feedback consists in segmenting the demonstration into primitives (e.g. “take object”, “move object” and “place object”) and in focusing retraining on the unsatisfactory ones only. This method has a broad prevalence in recent research, for example see Wu et al. [2014] and Jain and Inamura [2014]. Jain and Inamura used IL in a sophisticated setting. The robot received demonstrations for different tasks, like nailing or cutting. The robot has to discriminate the demonstrated tasks (e.g. “Beat the nail into the wood”) and determine which tool is useful for the task (“Use a tool with a large mass”), how to orient the tool (e.g. “Use the head of the hammer, not the grip”) and how to use the tool (“Hit the hammer towards the nail”). Vision is used to extract the properties of a tool: form, size and area of the effective part of the tool. After learning how to use the tools, the robot has to perform a similar task with a different tool. This is done to test whether the robot has correctly learned the important functional features of a tool (e.g. the blade of a knife or the head of a hammer) and is able to choose a good strategy for the available tool, the task and spatial constraints. If the reproduction fails or is not good enough, the robot makes a query to the demonstrator to solve the current task with the given tool. This approach was tested successfully with pulling an object towards the robot by first using a stick, then a T-shaped tool
and finally rakes, where the robot had to decide which rake to use, depending on the distance to the object [Jain and Inamura, 2014].

### 3.1.2 Models

The use of IL requires special consideration about the learning method. A great number of studies, for example the work done by Calinon and Billard [2007] or Cho and Jo [2013], use Gaussian Mixture Model (GMM) as the underlying model to encode demonstrated tasks.

However, GMM has two drawbacks when used for incremental learning: Firstly, the model cannot be updated, but needs to be relearned and secondly, the number of Gaussian components, as described in Section 2.2.2 needs to be defined beforehand ([Cederborg et al., 2010, Cho and Jo, 2013, Wu et al., 2014]). The first drawback is computational expensive, while the second one reduces the flexibility of the model. Over recent years much research has been published about improving GMM for incremental learning.

Kristan et al. [2008] proposed an approach to incrementally add new samples to a GMM and remove old samples if necessary. With this approach it is possible to not only add new information to the model, but also remove erroneous information, which could have been introduced by a poor demonstration. The advantage of the approach is that it is not necessary to tune parameters for specific applications, the form of the probability function can be arbitrary and no time constraints are assumed. The disadvantage is that it was only tested for one dimensional problems and needs to be extended for multi-dimensional learning tasks. Cho and Jo [2013] proposed a method where the trial data is abolished once used and the number of Gaussians is refined after each trial. The temporal normalization with DTW makes it possible to compare the trajectories of different demonstrations of the same task. Evaluating the pattern similarity enables the robot to autonomously assess the quality of a teaching trial and to reject demonstrations that differ too much from the other demonstrations. This method ensures that no false information by erroneous demonstrations are introduced to the model. Cederborg et al. [2010] described an “Incremental, Local and Online formulation of Gaussian Mixture Regression (ILO-GMR)”. This approach allows to not only learn incrementally new tasks, but also sev-
eral tasks at once. Every task is assigned to a certain environment. If the environment changes during the demonstration, the system recognizes, that a new task is shown. Correspondingly different tasks are reproduced according to the environment. The advantage of this approach is its flexibility. A whole workflow can be taught to the robot with the possibility to refine single steps with additional demonstrations.

HMMs in their original form have the same two drawbacks as GMM, as the model can not be updated and the number of states needs to be defined beforehand. HMMs can handle spatial and temporal variabilities of human demonstrations well and are thus, with some modifications, an interesting solution for IL [Calinon et al., 2010a]. Khreich et al. [2012] surveyed how on-line learning techniques are used for HMMs to incrementally learn the parameters. Different approaches, like incremental versions of the EM algorithm, exist. Kulic et al. [2008] used HMM to segment motions and incrementally cluster them, based on distances measured with log likelihood. Every motion primitive is added to a hierarchical tree and represents a group of similar motions. All observed motions are encoded into a HMM, compared with existing motion primitives and grouped with the closest primitive. Local clustering is then performed on the modified group. If a subset of motions similar enough is found, this subset forms a new group, therefore a new primitive. Utilizing this method, the system learns incrementally based on the observations. Dawood and Loo [2014] proposed the Topological Gaussian Adaptive Resonance Hidden Markov Model, where the data from the demonstration is processed into a topological map, which is used to update the state structure of the HMM. The remaining parameters of the HMM are learned with an incremental EM algorithm. This approach solves both drawbacks. The topological map defines the number of states, thus the number of Gaussians does not need to be predefined and the modified EM algorithm provides on-line learning for all other parameters.

3.1.3 Teaching various stiffnesses

Recent development in industrial robotics yields robots with controlled stiffness like the KUKA LWR4+, as described by Bischoff et al. [2010]. IL is used in combination with controlled stiffness in two ways. First, it enables the instructor
3.1 Incremental Learning

to move the robot during the reproduction to refine the task, as it will be shown in the course of this thesis. Second, the system can be trained on multiple trajectories in which different portions of the different demonstrations can be very similar or highly variable. This information can be used to tune the robot’s stiffness during replication of the task.

Calinon et al. [2010b] proposed a compliance controller that is compliant in intervals of the trajectory where the variance among demonstrations is limited (this is meant to model portions of the task that pose crucial constraints on the execution) and relatively soft where the variance is small. The general goal of this approach is to enable robots to work in unstructured environments (e.g. human workplaces) in contrast to controlled production lines. In unstructured workspaces the relationship between robot, tool and environment tends to be unpredictable and variable for each trial. Nevertheless, a compliant manipulator can assure sufficient contact force, as shown by Calinon et al. [2010b] based on an ironing task. The manipulator could effectively press the iron on a plate, independent of the reciprocal position of iron and plate, without exerting harmful forces. A further result of the approach is to ensure safety for the human worker by controlling the stiffness of the robot. The robot is operated within a sequence of possible different danger levels. To assess the current danger the distance between the robot and a human is measured and the viewing angle of the human is determined by head tracking. The highest danger level occurs when the user is close to the robot and facing away. The level is lower when the user can see the robot or the robot is further away. The robot replicates the task slowly and tries to find trajectories to avoid the user if the level is high, while reproduction at a low danger level is fast and with the nominal trajectory.

Using the variance as a parameter for the stiffness makes it also possible to teach compliant behavior to the robot. Kronander and Billard [2012] described a method to incrementally teach certain stiffnesses to certain sections of a trajectory. The use of compliant behavior is described with a pouring task and with lightening a match. Transporting a bottle of soda to an empty glass should be compliant, to avoid aggressive response to perturbations, while during the pouring the manipulator should be stiff to avoid missing the glass. A good example for the benefit of compliance for in-contact tasks is lightening a match. On one hand a stiff robot might use too much force and break the match or use too less force to generate the needed friction. On the other hand is exact
position tracking difficult for a compliant manipulator. Thus the robot is taught the motion of moving toward the matchbox and of striking the match. In reproduction the robot is incrementally taught to remove the compliance during the matching by wiggling the elbow of the robot, increasing the variance. The result was a 85% success rate instead of only 15% with both only high or only low stiffness.

Lee and Ott [2011] used variable stiffness to create a motion refinement tube. The motion refinement tube is the implementation of an impedance controller that prevents the instructor from giving demonstrations too divergent from the other demonstrations by setting the stiffness according to the variance of the model. A high variance at a certain point along the trajectory will result in a low stiffness at that point during the demonstration. Respectively a small variance will result in a high stiffness. Furthermore it is ensured that only parts of the robot are moved, which are necessary for the refinement, for example accidentally moving the torso when motions of the arm are refined. This property is implemented by setting a higher stiffness to joints closer to the base [Lee and Ott, 2011].

Another interesting approach that combines incremental learning and high compliance of the robot was described by Saveriano et al. [2015]. The goal was to exploit redundant DOF of a redundant robot to execute end-effector tasks, e.g. following a trajectory, and null-space tasks, which use the redundant DOF, at the same time. Instead of an impedance controller, as in [Lee and Ott, 2011], a task transition controller was implemented. First, the end-effector task is trained with kinesthetic teaching. Second, the task transition controller starts the execution of the trained motion primitive and detects interactions of the user by measuring external forces. These interaction forces are used to generate a new task. Such a task could be a certain elbow motion of a robotic arm to avoid an obstacle during execution of the end-effector task. Thus, a certain robot motion can not only be trained and refined, but also adapted to new constraints, like obstacles. The adaption uses the redundant DOF of the robot and hence it does not disturb the previously learned motion.
3.2 Reinforcement Learning

Reinforcement Learning (RL) is an unsupervised trial-and-error approach. Instead of supervising the robot and refining its actions, the robot is enabled to explore its own environment and find better ways to solve a task. The integration of RL with PbD is useful in cases where the demonstration is not sufficient enough to fulfill a task, for example due to big changes in the environment or suboptimal demonstrations. The combination of both is also useful to limit the search space for possible solutions, as further described in Section 3.2.3. With RL the robot can learn a way to reach its goal autonomously by trial-and-error exploration of its environment and exploiting explored actions to accumulate reward, specified by a reward function.

3.2.1 General idea of RL

The core of each RL approach is the reward function, which maps for every state-action pair a reward. A state is a vector with all current information about the system, for example position and velocity, which can be used to predict future states. The set of all existing states of the system is called state-space. The goal is to accumulate as much reward as possible. One of the main challenges in RL, after defining a reward function, is to define how to accumulate this reward. Depending on the assigned value for each state, certain actions are chosen to reach the next state. An action is a transition between states, in robotics this can be a control signal. The mapping between states and actions, e.g. which action is chosen for a certain state is called the policy. A greedy algorithm is trivial and will always choose the next state with the highest reward. More sophisticated approaches will also take the rewards of upcoming states into account. This happens with a value function, which maps for every state an additional value. While the reward expresses what is immediately beneficial, the value specifies what is beneficial in a long term. The value is an estimation of how much reward can be accumulated starting from that state [Sutton and Barto, 1998]. In contrast to plain PbD, the policy is not obtained from the demonstration, but through exploration of possible alternatives [Argall et al., 2009]. The values of the states are added, the path through the different states yielding the highest reward will lead to the execution of the desired task. The
3.2 Reinforcement Learning

The goal is to obtain a policy which results in such an execution [Argall et al., 2009] [Sutton and Barto, 1998].

Additionally to finding a policy, another challenge of RL is the trade-off between exploration and exploitation. On one hand the robot needs to try different actions to know which actions lead to success. On the other hand the robot needs to exploit those actions to accumulate the reward. Without exploration, no exploitation is possible. Without exploitation, no reward will be accumulated [Sutton and Barto, 1998]. Exploration is time consuming and it is necessary to limit it to an extent that the system is able to find effective actions which can be exploited. Complex systems like humanoid robots have huge state-spaces. One role of PbD within RL is to limit the state-space to states important for the task.

3.2.2 Early Work

Research for RL in robotic applications started in the 1980s with the goal of a general refinement of robot motor skills [Franklin, 1988]. Extensive research was done by Sutton and Barto [1998] who gave an overall description of RL, different methods how to obtain the policy and approaches to combine these methods. The main solution methods are Dynamic Programming, Monte Carlo Methods and Temporal-Difference Learning. Sutton and Barto distinguish between planning methods, that need a model of the environment, and learning methods, that can be used without such a model. A drawback is the inefficiency for high dimensional cases. With the increase of dimensions, the state space grows exponentially, which was called the “Curse of Dimensionality” by Bellman in 1957 [Sutton and Barto, 1998]. Exploring the whole state space is computational too expensive, but this problem is reduced with initial demonstrations. RL can be combined with PbD by demonstrating the task and thus providing prior information. These information consists of which states are important for the task and which actions are useful for these states. This limits the state-space and only states close to the demonstrated states must be explored.
3.2 Reinforcement Learning

3.2.3 Reinforcement Learning as Post-Training Optimization

The principle of RL aided by demonstrations is that trajectories from a demonstration are learned and generalized and the parameters of the built probabilistic model are forwarded to the RL module. The calculated trajectories are then executed and if the goal is not reached, the RL module tries to find better parameters for the model. The demonstration highlights important states and actions to limit the state-space and reduce the amount of necessary exploration.

Over the past years different approaches attempted to lower the impact of the “Curse of Dimensionality” with initial demonstrations and better learning algorithms. Peters et al. proposed the Natural Actor-Critic (NAC) algorithm for applications utilizing humanoid robots with many Degree of Freedom (DOF) [Peters et al., 2003] [Schaal et al., 2004]. The demonstration is first encoded with DMPs (see section 3.2.3) and the weights of the learned function approximator are then improved by a reward function. The policy is obtained by a natural policy gradient, which is estimated by the NAC. This method was used with a 30-DOF humanoid robot to match template trajectories.

Based on the NAC algorithm, Guenter et al. [2007] developed an approach where RL is used to cope with unforeseen obstacles. In cases where the information provided by demonstrations is not sufficient to reach the goal (final position), the robot uses RL to learn how to avoid the hurdle and reach its goal. As it can be seen in Figure 3.2, the demonstration is encoded and generalized with GMM to obtain a single model trajectory. The parameters of the GMM are the input for the RL module. The RL generates a modulation variable, which feeds the Dynamical System, where the control commands are generated. Simulations assess whether the goal is reached and finally a trajectory is executed. If the task fails, another modulation variable is calculated by the RL module. The advantage of this approach is the usage of a simulation, as hundreds of trials with the real robot are not practical and time consuming. With this method a way around the obstacle can be learned within seconds. However, this approach requires a precise model to use simulation for learning behavior. Kober et al. [2013] pointed out that only for stable tasks the learned behavior can be applied to the real world. Perturbations like contacts or friction are hard to model, thus learning in the real world gives better results than simulations. As a consequence
simulations are not suitable for in-contact tasks, despite their advantage of fast learning. Thus RL for in-contact tasks has to be used with real world trials, which requires considerably more time.

In the work of Guenter et al. [2007] the demonstration was only a tool to limit the state space initially. In more recent research, Gräve et al. [2010] used demonstrations to highlight important states and respective actions. The proposed algorithm compares provided demonstrations with the current situation. If a demonstration was similar to the current situation, the best action for the current state from that demonstration is compared with the action the system would execute in the current state. If the two actions are too different, the algorithm asks for another demonstration. However, if the actions are similar enough, it is safe to let the robot perform RL and explore its environment. The advantage of this approach is the limitation of human demonstrations to cases where they are necessary. RL is used if new obstacles are presented and the deviation between demonstrated information and planned action is within a defined limit. With increasing number of demonstrations, the RL module could handle more situations by exploring. The goal was to pick up a cup, which was placed randomly in a 600 cm$^2$ workspace. Only 15 demonstrations were used to exemplify the task. A similar approach was chosen by Sakato et al. [2014]. This approach distinguishes between two cases. If there is an instructor giving a demonstration, the robot will follow the presentation and learn. If no demonstration is given, the robot will decide whether it will perform a reinforced action or a learned action, depending on the similarity of the current state with the demonstrated state.

Figure 3.2: The principle of RL as post-training optimization method (Source: [Guenter et al., 2007])
Two main topics in recent research are the creation of robots, suited for more complex tasks than pick-and-placing tasks, for example surgical robots, and the use of DMP. Calinon et al. [2014] worked on a surgical robot that can perform endoscopic surgery. First, a surgeon teaches a robot different via-points, which the robot has to reach without damaging close organs. The problem of teaching the robot is the different embodiment of the surgeon and the flexible octopus-inspired 9-DOF STIFF-FLOP robot. Thus an intermediate step is necessary. The intermediate step is to demonstrate the task on a stiff robot. Therefore kinesthetic teaching of the task is performed on a stiff 7-DOF Barrett WAM robot in gravity compensation mode. The demonstration of the surgeon is used to extract a reward function. Second, the STIFF-FLOP robot uses this reward function and performs the task, exploiting its variable body characteristics and exploring new solutions to find a good policy. The initial demonstration of the surgeon is deficient due to the different embodiment between the WAM and the STIFF-FLOP robot [Malekzadeh et al., 2013]. These flaws are compensated with the refinement by RL, as the STIFF-FLOP learns how to execute the task with its flexible body and reaches a skill level beyond the demonstration of the surgeon. This approach was tested in two experiments, one simulated in software, one performed in a chamber filled with balloons, representing organs. The robot was able to follow the via-points much closer after the refinement than by just imitation learning [Calinon et al., 2014].

3.2.4 Reinforcement Learning with Dynamic Movement Primitives

RL can be used to refine the initial demonstration by updating the weights, which are initially set with the demonstration [Nemec et al., 2012, Pastor et al., 2012]. Current development in learning algorithms with DMP are reward-weighted averaging algorithms like Policy Improvement with Path Integrals (PI$^2$) or Policy Learning by Weighting Exploration with the Returns (PoWER). These methods appear to be extremely effective and outperform gradient based algorithms like NAC. Gradient based algorithms have many parameters that have to be tuned to result in fast convergence. With reward-weighted averaging algorithms only the noise variance has to be selected [André et al., 2015, Nemec et al., 2012, Pastor et al., 2012]. PI$^2$ and PoWER, both a direct development
of the NAC, introduce noise into the policy parameters to create new possible solutions. These algorithms can be used to learn the weights and the goal state for the DMP. The biggest advantage of the combination of DMP and PI\(^2\) is that it does not need any model or cost function for learning [Pastor et al., 2012]. An improvement to PI\(^2\) is PI\(^2\)-CMA which also estimates a covariance matrix, which enables to learn inter-parameter relations to increase convergence speed [André et al., 2015]. Nemec et al. used the PoWER algorithm to teach a robot with two KUKA LWR arms to pour a certain amount of liquid in a glass, without detecting the current amount of liquid poured (only the motion of pouring was considered). Two demonstrations were used to generalize the task and reduce the dimension of the state-space and PoWER was used to optimize the volume of poured liquid, while minimizing the amount of spilled liquid for different goal volumes. The experiments demonstrated fast learning rates of the algorithm [Nemec et al., 2012]. Andrè et al. compared PoWERS and PI\(^2\)-CMA in simulation. The algorithms were used to optimize the walking velocity of a bipedal robot for different inclinations of the floor. In all tests, the PI\(^2\)-CMA resulted in higher velocities [André et al., 2015].

### 3.3 Discussion

IL can be utilized not only to adapt the skills of a robot to new constraints, but also to improve the skills. Frequently used statistical learning methods like GMM and HMM have to be modified to allow incremental on-line learning. Several approaches to overcome the need of predefining the number of Gaussians/states and incrementally learning the parameters of the model can be found in the literature. With the occurrence of robots providing controllable stiffness and force sensing, new possibilities to utilize IL arose. These possibilities consist of helping the instructor to give better additional demonstrations to refine the skill of the robot and also to teach the robot various levels of stiffness for different parts of the task. RL is one of the fundamental machine learning areas, which has been used for decades now. Despite its usefulness, its full potential has not been discovered yet. The STIFF-FLOP project leads the way in exploiting RL for optimizing the skill of a robot after the demonstration phase. Currently is RL in combination with Programming by Demonstration mostly used to cope
with unforeseen events during the replication of a task, instead of refining the skill to solve the task.

The use of IL or RL for in-contact tasks is barely researched. IL seems to be best suited to refine the skills of a robot for in-contact tasks because of its supervised manner. Using RL for in-contact tasks is challenging, due to the exploration that is necessary part of RL. The problem is that the robot has to test different forces between tool and workpiece, thus endangering itself and its environment. Therefore it is mandatory to find limits for the exerted force and possibilities to distinguish between wanted and unwanted contacts. Future research is needed to solve the question how to exploit controllable stiffness of robots for in-contact tasks and how to assist the instructor during the demonstrations.
Chapter 4

System

This chapter gives an overview of the soft-, middle- and hardware used to implement an intuitively usable assistance system for PbD tasks. First the hardware will be presented. This is followed up by a description of the different software and middleware components and how they interact with each other.

4.1 Hardware

The hardware setup consists of five components: The KUKA LWR4+ robot, an ATI Mini45 F/T sensor, the KUKA Robot Controller (KRC) with attached KUKA Control Panel (KCP) and an external computer. Figure 4.1 shows how these hardware components are integrated.

Foundation of the conducted experiments is the industrial robot KUKA LWR4+, which is shown in Figure 4.1. The LWR4+ is a kinematically redundant robot with 7 DOF and is thus able to perform dexterous movements, while avoiding singularities. Two properties make this robot well suited for implementing the proactive assistance: Its lightweight design and its torque sensors in every joint with an additional force sensor in the wrist. The robot weighs only 15 kg (LWR stands for lightweight robot), while still able to handle payloads of 7 kg. This property is important to make it manually movable for a human instructor and thus suitable for kinesthetic teaching as described in Section 2.1. Another feature of the design is the round appearance of the robot, reducing the risk of
injury for nearby persons. The second property is the robot’s ability to measure torques and forces, which has several advantages. On one hand, it allows active vibration damping to ensure high precision. On the other hand, it facilitates the lightweight design with a sagging compensation of the slim and elastic joints. The robot acts as a spring-damper system, where the desired position, stiffness and damping can be defined both for joint- and Cartesian space. To control this system, the LWR4+ is equipped with three control modes: Position control, Cartesian impedance control and joint impedance control. The control cycle rate is 3 kHz in every joint and 1 kHz overall, enabling to switch the control mode within 1 ms [Bischoff et al., 2010]. These frequencies make it possible to detect and react to contacts and collisions fast, which proves not only useful in the course of this thesis, but for general aspects of physical human-robot interaction, e.g. the safety of human and robot.

An ATI Mini45 F/T sensor is attached between the wrist of the robot and the tool and allows precise measurements of exerted forces and torques within a force range of 290 N in x- and y-directions, 580 N in z-direction and for torque a range of 10 Nm in all directions. The resolution is for the force 1/8 N in all directions and for torque 1/376 Nm in x- and y-direction, and 1/752 Nm in
4.2 Middleware

The creation of robotic applications can be simplified by utilizing middleware frameworks. In the course of this thesis two frameworks were utilized, namely the Robot Operating System (ROS) and the Open Robot Control Software (Orocos). The most commonly used framework is ROS, which provides several useful libraries and tools for controlling robots. It is modularly structured and thus easy adaptable to many different tasks. But ROS does not support hard real-time which is required for components of this thesis, e.g. for virtual tool dynamics. Thus Orocos is used for software components which require real-time handling. These frameworks are next briefly described.

ROS was created to help programming robotic applications without “reinventing the wheel” and to reuse software components which have been shared by universities, companies and individuals [Goebel, 2013]. Software components in ROS are called nodes and use a publisher-subscriber system to communicate with each other. Nodes can publish topics with certain message types and other nodes can subscribe to these topics to get published data.
Orocos is a toolchain which can be utilized to create real-time software for robotic applications. Software created with Orocos is structured in *components* and *deployers*.

![Diagram of Orocos component structure](image)

**Figure 4.2:** The structure of an Orocos component. (Source: Soetens [2012])

A component, abstractly described in Figure 4.2, executes one or several programs written in C/C++ or the Orocos Program Script (OPS) in a single thread. Orocos ensures lock free and thread safe communication within a single or distributed processes and deterministic execution time during this communication [Soetens, 2012]. The functionality of components is implemented in operations, which are plain C/C++ functions. These operations can be used by other components via operation callers. Communication between components is established with ports, which are defined for a certain message type.

A deployer is a file written in OPS and specifies the Orocos environment by including components, setting their *activities* and connections and starts the included components. Components can be defined as peers to each other, which is a prerequisite to use operation callers. Activities can be defined as periodic, non-periodic or slave activities which are triggered when other activities execute. The communication between components is set up as connections between ports. The deployer also offers a way to communicate with ROS by specifying a stream
from a port to a ROS topic, so that a ROS node can subscribe to the data of an Orocos port or publish data to the port.

### 4.3 Software

The implementation of the incremental assistance system requires a sophisticated software infrastructure that establishes a connection between the external computer and the robot, commands the robot and guides the user through the teaching process. The main components are presented in the following sections and as an overview in Figure 4.3.

![Figure 4.3: Overview of the software infrastructure](image)

#### 4.3.1 Fast Research Interface

The Fast Research Interface (FRI) was developed by KUKA Roboter GmbH [Schreiber et al., 2010] to provide direct low-level real-time access to the KRC and thus control the robot from an external computer. For the communication between KRC and external computer the User Datagram Protocol (UDP) is used with frequencies up to 1 kHz. The FRI is realized as a state machine providing two different modes: Monitor mode and command mode. The monitor mode allows to receive sensor and status readings from the robot, but not to command the robot. FRI is always in monitor mode when started. To be able to switch to command mode, a sufficient communication quality is required. FRI
4.3 Software

sends a sequence of messages to the external computer and waits for an answer to evaluate the quality of the connection. In case the timing meets the desired timing specifications, the user may switch from monitor to command mode. Within the command mode the external computer can not only receive sensor readings and status information, but also set the control mode of the robot, change parameters, for example stiffness or damping values and command the robot to certain positions and forces.

4.3.2 Learning Framework

Learning primitives from demonstrations requires a learning framework, as described in Chapter 2. For the assisted incremental learning approach proposed in this thesis, an implementation of the DMP framework was utilized. This implementation was initially implemented by Steinmetz [2013] in the course of his master’s thesis and is described there in detail. The imitation part of this existing framework, where learning and execution are implemented, has been largely utilized and extended where necessary. The learning framework consists of three phases: *Imitation, learning and execution*. In the imitation phase an *Imitator* object is created, which takes parameters, for example the prefix of the recorded files and parameters for the DMP, and creates a *Demonstration* object for every recorded trajectory. These demonstrations are then passed on to the learning class, which uses LWR to learn the parameters during the learning phase. These parameters are then the input for the DMP to calculate the next desired state. In the execution phase these states are interpreted, depending on whether they are represented in joint or Cartesian space, and then commanded to the robot.

4.3.3 Proactive Assistance

The usability of kinesthetic teaching is strongly dependent on the weight and thus the inertia, of the robot. The user has to overcome this inertia to move the robot, which can result in jerky or inaccurate movements in case of high inertia. To address this problem, virtual tool dynamics were implemented which reduce the effective inertia of the robot and thus the robot feels lighter and
more movable to the user. This sort of assistance was implemented within the Orocos component \textbf{ProactiveAssistance}. An implementation in Orocos was necessary to maintain real-time assistance and to avoid delays which would disturb the user during the demonstration. First, the component sets the robot in Cartesian impedance control, to be able to change the stiffness and damping and allow kinesthetic teaching. The internal control law of the controller is [Schreiber et al., 2010]

\[
\tau_{\text{cmd}} = J^T(k_c(x_{\text{FRI}} - x_{\text{msr}}) + F_{\text{FRI}} + D(d_c)) + f_{\text{dynamics}}(q, \dot{q}, \ddot{q}),
\]

where \(\tau_{\text{cmd}}\) is the commanded torque, \(J^T\) the transposed Jacobian, \(x_{\text{FRI}}\) the Cartesian setpoint position, \(k_c(x_{\text{FRI}} - x_{\text{msr}})\) the Cartesian stiffness, \(F_{\text{FRI}}\) the Cartesian force/torque, \(D(d_c)\) the damping term and \(f_{\text{dynamics}}(q, \dot{q}, \ddot{q})\) the dynamic model of the robot [Schreiber et al., 2010].

The exact dynamic model of the robot is not available, however it can be said that, if frictions are ignored, the general dynamic model of the robot is of the form

\[
J^T(M(x)\ddot{x} + C(x, \dot{x})\dot{x} + g(x)) = \tau_{\text{cmd}}
\]

where \(M(x)\) is the symmetric, positive definite inertia matrix, \(C(x, \dot{x})\) is a combined matrix for the Coriolis and centrifugal terms, \(g(x)\) is the gravity vector and \(\tau_{\text{cmd}}\) the commanded torque [De Luca et al., 2006]. \(C(x, \dot{x})\dot{x}\) and \(g(x)\) are part of \(f_{\text{dynamics}}(q, \dot{q}, \ddot{q})\), which, according to Schreiber et al. [2010], represents the dynamics of the robot. Placing the dynamic model in the control law gives

\[
M(x)\ddot{x} + C(x, \dot{x})\dot{x} + g(x) = k_c(x_{\text{FRI}} - x_{\text{msr}}) + F_{\text{FRI}} + D(d_c) + f_{\text{dynamics}}(x, \dot{x}, \ddot{x})
\]

It is assumed that \(C(x, \dot{x})\dot{x}\) and \(g(x)\) are equal to \(f_{\text{dynamics}}(x, \dot{x}, \ddot{x})\). Then it follows that

\[
M(x)\ddot{x} - k_c(x_{\text{FRI}} - x_{\text{msr}}) - D(d_c) = F_{\text{FRI}}
\]

Second, the component reads the measurements of the external forces and torques \(F_{\text{FRI}}\) from the F/T sensor inside the wrist of the robot. A factor \(\alpha\) is defined by which the measured force and torque is multiplied \((F_{\text{FRI}} := \alpha \cdot F_{\text{FRI}})\) resulting in

\[
\frac{1}{\alpha}M(x)\ddot{x} = F_{\text{FRI}} + \frac{1}{\alpha}k_c(x_{\text{FRI}} - x_{\text{msr}}) - \frac{1}{\alpha}D(d_c)
\]

The division of \(M(x)\ddot{x}\) by \(\alpha\) reduces the effective inertia perceived by the user and renders the robot easier to move.
This approach eases kinesthetic teaching noticeably. However, it presents a serious drawback for in-contact tasks. In fact, the friction between the tool and environment causes the tool to bounce, as the vibration caused by overcoming the friction is amplified by the system. To tackle this problem the ATI F/T sensor is utilized to detect contacts of the tool with the environment. If such a contact is detected, the Cartesian stiffness is increased in z-direction. The result is a “magnetic” effect, which keeps the tool in contact, until the user exerts force in negative z-direction, thus lifting the tool. This prevents bouncing motions effectively, while maintaining the possibility for the user to exert the desired force.

4.3.4 AssistanceController

The AssistanceController is the centerpiece of the software developed and tested for this thesis. It is implemented as a ROS node and offers three modes to the user:

- Training a new skill
- Add new demonstrations to an previous training
- Replaying the learned skill

Teaching the robot new skills incrementally is done with several demonstrations. First an initial demonstration is provided to the robot using ProactiveAssistance, as described in the previous section. This demonstration is recorded and an Imitator object is passed to the learning framework to calculate an initial model. The robot then sets itself back to the starting position and the first iteration of incremental learning begins. At the beginning of every iteration the stiffness of the robot is increased and the robot moves along the trajectory learned so far. This behavior constitutes help for the demonstrator in two different ways. With low stiffness settings the demonstrator perceives the robot moving slightly forward, which reduces the effort for the demonstrator to overcome the inertia and renders the robot less unsteady. With higher stiffness values the robot performs the task increasingly autonomously. The mental effort of the demonstrator is reduced from giving the whole demonstration and
ensuring that the positions and forces are demonstrated as desired to observing
the robot and correcting the behavior of the robot where necessary. Due to the
fact that every demonstration differs at least slightly from other demonstrations
in speed and position, the learned trajectories require an alignment. After ev-
ery demonstration the recorded trajectory is aligned in time with the previously
recorded trajectory by warping the timelines of both trajectories. The result are
two trajectories whose corresponding positions lay at the same points in time.
The procedure of the alignment is described in detail in Section 4.3.4. If the
user wishes to give more demonstrations, the next iteration starts. The AssistanceController
leads the instructor through this process while commanding
the robot, recording and aligning the trajectories and communicating with the
learning framework. Therefore, the controller can be divided into three parts: The finite state machine, imitation and Dynamic Time Warping (DTW).

State Machine

The state machine shown in Figure 4.4 consists of four states: Start, Record,
Add/Execute and End. After AssistanceController is started the state ma-
chine is in the Start state. In this state the user is presented with three choices:
1. training a new skill; 2. adding new demonstrations to the current primitive
or 3. executing the learned primitive.

In case the user chooses the first option, the state machine moves to the state
Record. In this state the system is in gravity compensation mode and the user
is prompted to move the robotic arm to a starting position. The recording of
the initial demonstration, aided with the ProactiveAssistance, starts imme-
diately after the user confirms the starting position. Once the demonstration
is done, the state machine switches into the Add/Execute state to start the
imitation and check whether the imitation was successful and whether the user
wants to record an additional demonstration or replay the skill. In cases where
the imitation could not be completed or where the user quits the program, the
state machine transits into the End state, where the state machine and hence
ProactiveAssistance is commanded to stop. If the user chooses the second
option thus resuming teaching of a skill from a point he stopped earlier, the
state machine transits directly from Start to Add/Execute, while defining all
necessary parameters, e.g. stiffness, to proceed from the desired point. If the
user wants to replay a learned skill without adding new demonstrations, they choose the third option in the **Start** state. Then the state machine transits from the **Start** state to the **Execute** state while setting a high stiffness.

**Imitation**

The imitation module is the implementation of the incremental learning approach and has two purposes: First, replaying the current model of the motion primitive while recording the demonstration of the user and second, setting the stiffness for the current iteration. The first aspect allows to physically guide the robot during the imitation of the motion primitive. The benefit of this approach is that the robot helps the user to overcome the inertia of the robotic manipulator, which results in more natural movements. Furthermore the user can concentrate on correcting the trajectory where it was not sufficient in previous executions. This reduces the complexity of teaching the skill. The latter purpose of the imitation module is to increase the stiffness of the robot incrementally. During the second demonstration, the robot moves autonomously according to the first demonstration. Therefore, the user can move the robot
more freely, assisted by the proactive behavior of the robot. The robot’s assistance grows incrementally after each demonstration, as the robot makes use of the previously received information, takes into account the user’s corrections and becomes more stiff. This process helps the user to incrementally focus on the necessary corrections rather than on the execution whole task, thus increasing accuracy. The stiffness value $S$ for the iterations is calculated as

$$S = 2^{i-1} \cdot 100 \frac{N}{m}$$

where $i$ is the current number of demonstration. A problem in incremental learning is that as the number of demonstrations increases, the relative weight of each demonstration becomes smaller. Therefore, the imitation module forgets old demonstrations and the learning framework utilizes only the last three demonstrations, which are weighed equally, to learn the parameters with LWR. After each imitation, the user has to temporarily pause the recording of new demonstrations and the imitation module will trigger the DTW module.

### Dynamic Time Warping

A problem that appears with the approach described above is the variability of human demonstrations. Each demonstration will differ from the other ones for speed, trajectories and forces, which renders problems for the learning framework. To reduce the impact of this problem, DTW has been implemented, to align the recorded trajectories with respect to time. The orientation of the tool is set when moving the robot to the start position. The force between tool and surface is coupled with the position, as at a certain point of the trajectory a certain force has to be applied. Therefore force values are stored together with the respective positions so that force-position pairs remain the same after the time warping. Thus only the trajectories are considered for the alignment. To align two trajectories $s$ and $t$, the algorithm first measures the distance between them by calculating the distances of every point of $s$ with length $N$ to every point of $t$ with length $M$. As the original DTW algorithm was developed for the one dimensional problems of speech recognition, the distance calculation had to be extended for three dimensional trajectories. The cost function was changed to $|(s_x - t_x)| + |(s_y - t_y)| + |(s_z - t_z)|$, which takes all three dimensions into account (line 8 in Algorithm 1 in AppendixA). These distances are saved in a $N \times M$-matrix. Second, a backtracking algorithm is used to find a path, called
warppath, through the matrix that yields the shortest distances [Müller, 2007]. Every item of the warppath can be referenced by its index inside the matrix. These indices are stored and used to warp the trajectories and align them. For better illustration, DTW algorithms are sketched in Appendix A. Calculating the distance matrix is shown in Algorithm 1, calculating the path in Algorithm 2 and the warping process in Algorithm 3. With this warping process the length of the warped trajectories equals the length of the warppath and is longer than $s$ or $t$. The more warping is required, the longer the warppath and the resulting trajectories are. This stretching of the trajectories results in parts where the position remains constant. To avoid that the robot stagnates at positions where it should keep moving these expendable parts are removed from the warped trajectory. An issue that might result from this approach, although it has not been observed so far, is that the execution speed might clearly differ for parts of the trajectory than the speed during the demonstration.
Chapter 5

Experiments and Results

Evaluating physical human-robot interaction is a challenge as quantitative measurements reveal the performance of the robot, but also the human side has to be considered. Therefore, the evaluation of the assistance system is done in two parts. The first part will show the benefit of the assistance on learning different geometrical shapes. The second part will utilize a user study to evaluate how intuitive and easy the system is to use and how novice users interact with the system.

5.1 Quantitative Evaluation

A quantitative evaluation of the implemented system is difficult, as the capability of the user to kinesthetically teach a task has a severe influence on the resulting learned primitive. First, the influence of DTW on the learned skill will be investigated on an example of a single teaching trial of teaching the robot to draw a square. Then drawing a square and a circle were chosen as tasks to show the performance of the system. Drawing a square, which requires straight lines and sharp angles, can show the behavior of the system in cases where the desired primitive has sudden changes of direction. Drawing a circle is a relatively difficult primitive, as a constant radius has to be maintained, and thus suitable to reveal the impact of the assistance compared to unassisted training. To cope with the difference in position over several demonstrations, every teaching trial
5.1 Quantitative Evaluation

was performed ten times to reduce the impact of the human influence and to give meaningful results.

5.1.1 Dynamic Time Warping

The implementation of DTW was necessary as the difference in speed during demonstrations results in a poor replication of the primitive. This is due the fact that the learning system outputs the mean of the learned trajectories. The

![Figure 5.1: The learned motion primitive of the same demonstrations with DTW and without DTW.](image)

assisted incremental system was used to program a square with kinesthetic teaching. Five iterations were performed, the first one fully compliant with virtual tool dynamics and then with increasing stiffness \((200 \, \text{N/m}, 400 \, \text{N/m}, 800 \, \text{N/m}, 1600 \, \text{N/m})\). The recorded trajectories were saved in their original form and, from the second iteration on, time-aligned with the previous demonstration. The resulting primitive, learned from the last three demonstrations, was replicated twice with a stiffness of \(4000 \, \text{N/m}\), once using the original trajectories and once using the DTW-aligned trajectories. The difference can be seen in Figure 5.1. It is apparent that the square primitive extracted using DTW (blue square) shows distinct corners. On the opposite, the primitive learned from non DTW-aligned trajectories, although extracted from the same set of demonstrations, does not
capture the quality of sharp corners. The corners are rounded and changes in direction occur too early. This emphasizes the importance of trajectory-alignment for incremental learning approaches.

5.1.2 Training the robot to draw a Square

The goal of this experiment was to measure the influence of the assistance on the end result compared to teaching trials performed without assistance in gravity compensation mode. To express the result in numbers the mean square error was chosen, which is the distance of the result compared to a perfect square.

Experiment

In order to get comparable results, a template square was programmed in KRL, representing a hardcoded trajectory. The four corner points of the template were marked on sheets of paper with 10 cm distance between them, as displayed in Figures 5.2 and 5.3. Then the robot was trained by the author of this thesis to draw a square on the prepared paper sheets with a standard marker, whose tip had a diameter of 4 mm. The experiment consisted of ten teaching trials in gravity compensation and ten teaching trials with the assistance system. The assistance system used virtual tool dynamics and set the robot fully compliant for the initial demonstration. Four iterations were performed with stiffness values of $200 \, \frac{N}{m}$, $400 \, \frac{N}{m}$, $800 \, \frac{N}{m}$ and $1600 \, \frac{N}{m}$. The teaching trials in gravity compensation were performed by grabbing the robot by its wrist. The initial demonstrations for the assisted trials were also performed by grabbing the robot by its wrist. This was necessary to not disturb the force readings of the ATI F/T sensor in z-direction so that the detection of contacts work (see Section 4.3.3). However, as the increased stiffness during the iterations prevent the tool from bouncing over the surface due to friction, the ATI F/T sensor was used to measure the interaction between the human and the robot more precisely. Therefore all iterations after the initial demonstration are performed by grabbing the tool directly.
5.1 Quantitative Evaluation

Results

The result for the teaching trials in gravity compensation mode can be seen in Figure 5.2, which shows the result of the ten teaching trials in gravity compensation mode (orange) to the template (blue). It is apparent that it is hard to move the robot only in the desired direction to connect the marked points with straight lines. The teaching trials were performed clock-wise, starting at the upper right corner and ending in the same point. Directly after the start large jerky deviations from the template are visible, as the inertia of the robot had to be overcome. To draw a straight line a robot needs to perform a synchronized movement of several joints. Kinesthetic teaching without assistance results in the passive movement of several joints that prevents the achievement of a smooth movement for the user steering the robot. The mean distance of all trajectories trained in gravity compensation from the hardcoded perfect square was $2.16 \pm 1.10 \text{ mm}$. Figure 5.3 reports the results achieved with the incremental assistance system. The mean distance to the template was $1.96 \pm 0.84 \text{ mm}$. The first teaching trial had a mean distance of $3.4 \text{ mm}$. If this result is omitted as an outlier, the mean distance of all results from the template would be $1.80 \pm 0.53 \text{ mm}$. Taking the size of the tip of the pen into account and that only the corner points were marked, that is a very close result to what was pro-
Figure 5.3: The replications of ten teaching trials with the assistance system compared to the template

grammed in KRC. The assistance system shows its strength in comparing the straightness of lines. It is apparent that the squares were much straighter than the results trained in gravity compensation mode. Training with the assistance system results in squares much more similar to the template, while showing straighter lines and more distinct corners.

The impact of the assistance can be seen clearly in Figure 5.4. The initial demonstration is very jerky, barely displaying any straight parts. However, after assisted training, the overall performance has clearly improved. The whole progress of an assisted trial, from the initial demonstration to the result, can be seen in Figure 5.5. Figure 5.5 also visualizes the interaction between human and robot. A general problem with using the force data is that the F/T sensor does not only measure the forces exerted by the user. As the pen is attached to the ATI F/T sensor, forces that occur at the tip of the tool due to friction are measured too. Using the F/T sensor in the wrist is no solution as the readings from that sensor contain also the forces exerted by the robot itself. To give a clearer figure of the interaction between the robot and the human, the force component that is not parallel to the movement of the robot was calculated. This force component better constitutes the correctional forces exerted by the
Figure 5.4: Comparison of initial demonstration and result

user. Nevertheless, this solution is not perfect, as it can be seen in the plot of the result. This last plot depicts the replication of the skill without involvement of the user and therefore shows the forces perpendicular to the movement solely exerted by the robot. Despite the mixture of origin for the measured force, the user part can be recognized in higher force readings, represented by longer arrows. It can be seen that the overall amount of exerted forces decreased with progress of the teaching trial and forces were exerted more punctually for correction purposes. This confirmed that the behavior of the user changed from giving the whole demonstration on its own to just guiding the robot and correcting where necessary.

5.1.3 Training the robot to draw a Circle

A further experiment was conducted, comparable in terms of modality and complexity, to study the impact of the assistance system on a relatively difficult task.
Figure 5.5: Progress of an assisted teaching trial of a square. It can be seen how the trajectory becomes a better square and the correctional forces that have been applied. Correctional forces applied towards the left side of the movement direction of the robot are marked green, forces applied to the right side are marked red.
5.1 Quantitative Evaluation

Experiment

Similar to the previous experiment, a circle was programmed in KRL to have a reference. This reference was used to mark four points on paper, which lay on two perpendicular lines, to denote the dimensions of the circle, which had a radius of 4.9 cm. For better clarity the markers are displayed in Figure 5.6 and 5.7. Then ten circles were trained in gravity compensation mode and afterwards ten teaching trials with the assistance system were performed. The distance measurement was also chosen as a metric for this experiment. Combined with visualizations of the results it gives a good impression of the improvements.

Results

The results of the teaching trials in gravity compensation mode can be seen in Figure 5.6. The task is harder than the previous one, as apparent from the comparison of Figures 5.2 and 5.6. In fact, the shaky curves that barely make their way through the given marks could hardly be called circles. At the uppermost part of the circle the results exhibit a smaller deviation from each other. However, around the remaining marks the drawn curves lay within a range of 1 cm apart. This result can also be expressed in the mean distance from the template, which is $5.68 \pm 4.78$ mm. The high standard deviation is a particularly eloquent indicator of the inaccuracy of teaching trials in gravity compensation.

Better results were achieved with the aid of the assistance system, as can be seen in Figure 5.7. Although still far from perfect circles, the drawn curves were much closer to the suggested template. The top, bottom and left marks were met fairly close (considering the tip size of the pen). This was also reflected in the mean distance from the template of $3.18 \pm 1.91$ mm. This shows that with the aid of the assistance the user was able to draw significantly more accurate circles.

An example of the gap between initial demonstration and result, and thus the impact of the assistance system, can be seen in Figure 5.9. The general impression that the use of the assistance system results in rounder circles is affirmed. A whole teaching trial during assisted training, with visualized perpendicular
5.1 Quantitative Evaluation

Figure 5.6: The results of the teaching trials in gravity compensation mode compared to the template

Figure 5.7: The results of the assisted teaching trials compared to the template
forces (similar to the previous case), can be seen in Figure 5.8. After the initial demonstration comparatively strong and consistent correctional forces are applied during the first iteration. During the second iteration correctional forces are mostly applied immediately after the start of the demonstration. In the following demonstrations most of the force was exerted at the end point. The force reading of the result shows the forces measured during reenactment of the learned task by the robot alone, i.e. without any direct interaction with the user.

5.2 Qualitative Evaluation

To evaluate how easy and intuitive the system is to use and to understand how novice users perform with the system, a user study was conducted, inspired by the study performed by Wrede et al. [2013]. Ten participants performed the test in two cases and were asked to take part in a survey afterwards. One participant was excluded from the analysis as a failure occurred during the teaching trial. The remaining participants were aged between 23 to 28, of whom six were males and three females. The origin of the participants is highly diverse with participants from Germany, Netherlands, India, Bangladesh, Spain and China. The exact composition of origin and educational level is reported in Figure 5.10. Seven participants stated they have prior experience with robots, of whom five have experience with robotic arms, one with robotic hands and one with simulated robots. Six participants rated their manual skills as good, while three stated they have bad manual skills.

Five hypotheses were tested:

- The assistance system is easy to use
- The assistance system is not perceived as threatening
- User have a better overall experience with the assistance system
- The robot is easier to handle with the assistance system
- The results are more accurate with the assistance system
Figure 5.8: Progress of an assisted teaching trial of a circle with correctional forces visualized. Correctional forces applied towards the left side of the movement direction of the robot are marked green, forces applied to the right side are marked red.
5.2 Qualitative Evaluation

5.2.1 Setup

The study was divided into four parts. First, both cases were demonstrated to show the participants how to use the robot. In the second part, the participants had the possibility to try both cases on their own. For case A the robot was in gravity compensation mode and participants could move the robot freely. To get acquainted with the gravity compensation the users were asked to draw two squares. For case B the users were asked to draw a square using virtual tool dynamics fully compliant (i.e. the robot actively follows the force applied by the user) and then with a stiffness of 400 $\frac{N}{m}$, so the user acquired a feeling for the system. After this warm-up phase both cases were tested in teaching trials. As all participants were new to the system, learning effects have to be taken into consideration. Therefore half the participants started the teaching trials with case A, the other half with case B. This procedure was necessary to avoid biasing
5.2 Qualitative Evaluation

the results towards the case tested last. For comparability the users were asked
to train the robot to draw a square and the corner points of the square were
marked on the paper where the participants drew on. For case A the users were
asked to train four squares in total in gravity compensation. The user had a free
choice where to grab the robot, but all participants grabbed the robot at its wrist
(as it was demonstrated in the first part). Then the recorded trajectories were
batch learned with the DMP framework and the result shown to the participant.
For case B the participant was asked to give an initial demonstration by grabbing
the robot at its wrist and then three additional demonstrations with stiffness
values of $200 \frac{N}{m}$, $400 \frac{N}{m}$ and finally $800 \frac{N}{m}$. The last three demonstrations were
performed by grabbing the tool directly. Then the result from this teaching
trial was presented to the user. The last part of the study consisted of a survey,
that consisted of questions about the participants, both cases and a general
comparison. The questions and the results are described in Section 5.2.2.

5.2.2 Results

The analysis of the results is divided into two parts. In the first part the result
of the survey will be analyzed while the second part considers the result of the
teaching trials. For most questions, participants were asked to give a rating
of 1-5 with 1 as very bad or strong disagreement to 5 as very good or strong
agreement. To better compare the results between case A and B a statistical
hypothesis test, namely the Wilcoxon Signed-Rank Test [Wilcoxon, 1945], was
performed.

Survey

The rating of the simplicity of the system was $4.00 \pm 0.87$ in case A and $4.33 \pm 0.71$
in case B with a p-value of 0.5625 as displayed in Table 5.1. The intuitivity was
rated with $3.78 \pm 0.83$ and $3.89 \pm 0.93$ and has a p-value of 1.0000. This reflects
that teaching the robot a new skill is perceived within the participants as a bit
simpler with the assistance than without, while there is almost no difference in
terms of intuitivity. For both ratings no statistical significance can be identified.
A greater difference was perceived in the quality of the result. The result with
gravity compensation was rated $3.67 \pm 1.22$, while the result achieved with the
5.2 Qualitative Evaluation

Figure 5.10: Distribution of origin and educational level of participants

Figure 5.11: Answers for the question whether the intensity of assistance should change

<table>
<thead>
<tr>
<th>Question</th>
<th>Case A</th>
<th>Case B</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simplicity of handling</td>
<td>4.00 (0.87)</td>
<td>4.33 (0.71)</td>
<td>0.5625</td>
</tr>
<tr>
<td>Did the handling feel intuitive</td>
<td>3.78 (0.83)</td>
<td>3.89 (0.93)</td>
<td>1.0000</td>
</tr>
<tr>
<td>How would you rate the result?</td>
<td>3.67 (1.22)</td>
<td>4.22 (0.67)</td>
<td>0.3125</td>
</tr>
<tr>
<td>Was the handling physical demanding?</td>
<td>1.89 (1.05)</td>
<td>2.11 (1.27)</td>
<td>0.5000</td>
</tr>
<tr>
<td>Was the handling mentally demanding?</td>
<td>1.78 (1.30)</td>
<td>2.00 (1.32)</td>
<td>0.7500</td>
</tr>
</tbody>
</table>

Table 5.1: Mean results for the experience in both cases A and B
5.2 Qualitative Evaluation

<table>
<thead>
<tr>
<th>Question</th>
<th>Mean</th>
<th>SD</th>
</tr>
</thead>
<tbody>
<tr>
<td>How would you rate your manual skills?</td>
<td>3.33</td>
<td>1.00</td>
</tr>
<tr>
<td>Was the assistance helpful?</td>
<td>4.56</td>
<td>0.53</td>
</tr>
<tr>
<td>Did the interaction with the robot feel awkward/threatening?</td>
<td>1.56</td>
<td>0.53</td>
</tr>
</tbody>
</table>

Table 5.2: Additional statements of the participants

assistance was rated 4.22 ± 0.67. The variance shows that the participants were less certain how to rate the result in case A and also gave it a worse rating. In case B the result got a distinctively better rating with a higher certainty. The difference between the ratings of the result is indicative of an improvement but with a p-value of 0.3125 not statistically significant. Both physical and mental demand were rated a bit higher for the assistance system with 2.11 ± 1.27 and 2.00 ± 1.32 over 1.89 ± 1.05 and 1.78 ± 1.30. Also in these both cases are the difference not statistically significant. In general, the assistance was perceived as very helpful with a rating of 4.56 ± 0.53. 33% of all participants wished the robot would help more, 56% stated that the assistance is good as it is, while 11% would have preferred less help. For better clarity these results are summarized in Table 5.1 and 5.2 and Figure 5.11.

**Teaching Trials**

The teaching trials of the participants were recorded to be able to evaluate the performance of the system when utilized by novice user. The four demonstrations given without assistance were batch learned and the learned trajectory executed and recorded. These results can be seen in Figure 5.12. Figure 5.13 shows the results which were achieved with the aid of the assistance system. Despite the fact that the trajectories trained in gravity compensation mode were batch learned and thus every plotted result is the mean of four demonstrations, the lines are unsteady and curved. On average the assistance helps the user to give better demonstrations. The results lie closer together and the lines are mostly more straight. This is also reflected in the mean distance of the trained trajectory from the template. Unassisted teaching trials result in a trajectory which has an average distance of 5.09 ± 3.68 mm while the usage of the assistance results in a distance of 2.96 ± 2.50 mm. Altogether the results of case B
5.2 Qualitative Evaluation

Figure 5.12: Learned trajectories based on the teaching trials of novice users in gravity compensation mode

Figure 5.13: Learned trajectories based on the teaching trials of novice users aided with the assistance system
are closer to a square than the results of case A. However, a distinct difference to Figure 5.3 is visible. The teaching trials of Section 5.1 were performed by an experienced user, thus the difference is attributable to a different level of experience with the system. Nevertheless it can be stated that a distinct improvement of demonstrating skills to the robot can be achieved by novice user who use the system for the first time. The results described in Section 5.1.2 suggest that an even greater improvement is possible if the user has more time to get acquainted with the system.

5.3 Discussion

The conducted experiments presented in this chapter show clearly an improvement of programming a skill by demonstration with the assistance system over unassisted teaching trials. The quantitative evaluation shows that an experienced user can achieve results for a drawing task that can be close to the hard-coded template. To explore the interaction between robot and novice users, a user study was performed that showed a distinct improvement in the quality of the learned skill, which can be achieved without prior experience with the system or the particular robot.

Part of the quantitative evaluation was the demonstration of the necessity of an alignment of demonstrated trajectories. However, the utilized DTW algorithm is only designed to work with two trajectories. This yields a problem that emerges when the results of novice user are analyzed. Despite the use of DTW, most results exhibit rounded corners. This is due the fact that trajectory $t_1$ gets aligned with trajectory $t_2$ and, after the second iteration, the resulting alignment $t_{12}$ with trajectory $t_3$. The alignment of $t_{12}$ and $t_3$ is denoted as $t_{23}$. Naturally there is a discrepancy between the alignments $t_{12}$ and $t_{23}$, which is smaller than the discrepancy between $t_1$ and $t_3$, but can be big enough to result in a smoothening of sharp changes of direction. The conclusion is that DTW can improve the quality of a trained skill greatly, as shown in Section 5.1.1, but has its limits if demonstrations differ highly in timing.

To illustrate the impact of the assistance system two different primitives were trained by an experienced user with and without the assistance system. It
is apparent that it is hard to train new skills in gravity compensation without further assistance, as the resulting trajectories tend to be unsteady and far away from desired positions. However with the aid of the assistance system results were achieved that are at least better than the results achieved with gravity compensation, for example at teaching the robot to draw circles, or even close to perfect representations of the primitive, in the case of drawing a square.

During the user study five hypotheses were tested. The first three were that the assistance system will be perceived as easy and intuitive to use and that the interaction with the robot will not be perceived as awkward or threatening. The expectations were fulfilled within the participants. The assisted system got a better rating than the unassisted method in terms of simplicity. There was almost no difference between the intuitivity of case A and B, however, both were rated good. Another result is that no participant perceived the system as awkward or threatening. The other two hypotheses were that the users prefer the assisted system and achieve desired trajectories with it. This was confirmed by the better rating for the results of the assistance system and that the assistance system was rated very helpful, as the quality of the results improved noticeably. The perception of the improvement of programming a skill from the quantitative evaluation was reinforced by analyzing the teaching trials of the participants. On average the trajectories trained with the assistance system were more steady and closer to the hardcoded template than the trajectories trained without assistance.

However, the results of the user study have to be seen as indicative, as no comparison between case A and B exhibits statistical significance. Therefore a larger user study needs to be performed to confirm the aforementioned observations. Further improvements have to be done regarding the mental and physical demand. Despite rated as not very mentally or physically demanding, case B got a slightly worse rating than case A.

The last question of the user study was how the user would describe his or her experience with the robot and what should be improved. In general the users reported a positive experience while suggesting the implementation of additional cues during the iterations to indicate the pace of demonstration the robot assumes based on the previous demonstrations. One issue that appeared during the user study is that some users gave an initial demonstration slowly,
but increased the speed of demonstration as moving the robot is easier the more assistance is offered. The stiffness of the robot is defined as $\frac{N}{m}$, meaning it becomes harder to move the robot further away from its desired position. The desired position is calculated from previous demonstrations. The consequence is that users who gave distinctly faster demonstrations than previous demonstrations ended up pressing against a resisting robot. Users more experienced with the system tended to have a better feeling for guiding and giving corrections to the robot. Two participants stated that the robot was at some point hard to move and one of them suggested smaller stiffness values for the assistance. As the tested values were relatively low it might be a good approach to increase the stiffness of the robot in the direction of movement, to make the guidance more obvious, while having less stiffness in transversal direction.

The system is currently limited to use the same orientation that has been set after moving the robot to the start position. For the aforementioned tasks this behavior reduces the mental demand as the user does not have to concentrate on keeping a desired orientation of the tool. Naturally, this is only feasible for tasks that do not require various angles between tool and surface. However, only a factor in the ProactiveAssistance component has to be changed to allow varying orientations during the demonstrations. So far, the system was only tested for drawing tasks on a flat surface. Nevertheless, an extension to allow more sophisticated tasks, e.g. planing, should not require much more than adjusting certain variables. An open question is how the system would perform for tasks that requires a certain timing, e.g. playing an instrument. The current implementation of DTW has a similar execution timing, i.e. which movements are performed at a certain point of time, than the demonstration timing, yet the difference and possible implications have to be tested.
Chapter 6

Conclusions

The goal of this thesis was the creation of a system to assist users in providing better demonstrations of a skill to a robot and thus allowing a user to train a robot in an easy, intuitive and flexible way, especially for skills that are hard to program because of contact forces, uncertain and unstructured scenarios and similar reasons. From the analysis of the general framework of PbD, Incremental Learning stood out as a promising method to assist and facilitate the user during demonstrations of the task, being complementary to the natural and intuitive user experience promised by PbD. Incremental Learning is suited for usage in an assistance system, as it is a supervised method that allows a user to improve the trained skill where necessary, while having control over the forces exerted by the robot. Accordingly, the system presented in this thesis was implemented as an incremental approach, extended with virtual tool dynamics, that provided increasing assistance with increased knowledge of the task. Finally, the system is evaluated with respect to its performance, simplicity, intuitivity and usability by novice users. The experiments showed a distinct improvement of the primitives learned from assisted teaching trials over unassisted demonstrations for experienced users. Furthermore the user study revealed that the system is easy and intuitive to use and can also improve the demonstrations of novice users greatly.

The work of this thesis is based on the infrastructure implemented by Steinmetz [2013]. The contribution of this work is to extend the existing infrastructure to an assistance system. The implemented system is based on two main ideas with the aim to assist a user in giving better demonstrations. The first idea
was to reduce the effective inertia perceived by the user, making the robot easier to move. This was achieved by implementing virtual tool dynamics. The second idea was to utilize incremental learning to enable the user to physically guide the robot during the execution of tasks. This method allows to teach natural movements. Additional to assisting the user the system improves the quality of learned trajectories by using Dynamic Time Warping. Various paces during demonstrations result in a primitive that can be rather different from the intended primitive, e.g. distinctive elements like sharp angles are smoothed. Dynamic Time Warping was implemented to cope with this problem by aligning the demonstrated trajectories thus improving the quality of the learned skill.

The experiments reported in this thesis analyze both quantitatively and qualitatively the implemented approach. The quantitative evaluation examined the general performance of the assistance system. It was shown that the assistance system has a huge impact on the quality of the learned skills. The assistance system can help the user to train the robot in a way that the accuracy can be satisfactory once compared to results achieved by hardcoding the robot. The strength of the assistance system is twofold. It can be utilized by users without programming knowledge and assisted teaching trials are conducted more natural, simpler, faster and more flexibly than hardcoding the robot, even for comparably simple tasks like drawing basic geometric figures. Also teaching trials can be used to program a robot in cases not enough information is available for hardcoding, e.g. in in-contact tasks. The qualitative evaluation was performed in form of a user study to show that no knowledge of the particular robot or experience with the assistance system was necessary to achieve a swift and obvious improvement in the quality of the trained skill. The assistance system was implemented with the demand to be easy and intuitive to use, without being perceived as threatening. A further goal is to increase the accuracy of the training phase with respect to unassisted teaching trials. All these demands are positively addressed. However, a comparison of the results between an experienced user and novice users show that the system can be utilized more effective by experienced users. Nevertheless, it was shown that even just a few assisted teaching trials are sufficient to novel users to build a good feeling with the robot and remarkably improve the overall performance.

Not much research has been performed earlier to examine the possibilities of incremental learning in combination with kinesthetically teaching with state of
6.1 Future Work

Several aspects need to be improved in order to seamlessly integrate the system in a work environment.

One of these aspects consists on providing additional cues to the user in order to make the currently learned trajectory visible. This visualization could be done by projecting the trajectory onto the surface. Another aspect would
be the different pace of demonstrations. For every point in time during the demonstration, cues could be provided that denote the position of the tool at the same time in the previous demonstration. This could help novice users to utilize the system more efficiently as discussed at the end of Chapter 5. The user friendliness should also be improved by implementing a graphical user interface, which gives clear instructions to the user and allows an easy selection of different modes and saving and reloading learned skills. All the necessary functionalities have already been implemented, but they currently have to be controlled in a terminal.

So far the system has been tested on relatively simple tasks and it has yet to be shown that the system can also be generalized to more complex tasks. As the system is implemented to transfer skills from an expert in his field to the robot, future work would consist of testing the system with skilled participants for complex tasks and comparing the results of the teaching trials with results manually achieved, without the robot involved. It would be interesting to explore whether and how much the process of transferring complex skills from an expert to the robot can be improved by the use of the assistance system.

The results of the performed user study indicated an improvement of several attributes of the assisted system over unassisted teaching trials. However, a larger pool of participants is required to show that the reported observations are not only valid within the participants of this study, but are statistical significant. Furthermore could the assessment of additional data, e.g. time required to teach skills, provide a better insight in the advantages and disadvantages of the assistance system. An interesting aspect that could be investigated is the performance development of the participants, i.e. how the quality of the demonstrations is dependent on the experience with the assistance system.

Another possible area of future research would be to develop a method that extends Dynamic Time Warping to simultaneously time align several trajectories with each other. This would further increase the reproduction quality of skills trained with different paces, as the discrepancies between several alignments, which are discussed in Chapter 5, would vanish and reduce smoothing of the learned primitives.
References


REFERENCES


Appendix A

Dynamic Time Warping

**Input:** trajectory s,t  
**Output:** DTW  
$$\text{DTW} = \text{array}(N,M);$$  
$$\text{DTW}[0,0]=0;$$  
$$\text{for } i = 0 \text{ to } N \text{ do}$$  
$$\quad \text{for } j = 0 \text{ to } M \text{ do}$$  
$$\quad\quad \text{minimum} = \text{inf};$$  
$$\quad\quad \text{dist} = |(s_x - t_x)| + |(s_y - t_y)| + |(s_z - t_z)|;$$  
$$\quad\quad \text{if } i > 0 \text{ then}$$  
$$\quad\quad\quad \text{minimum} = \text{DTW}[i-1, j];$$  
$$\quad\quad \text{if } j > 0 \text{ then}$$  
$$\quad\quad\quad \text{minimum} = \min(\text{minimum}, \text{DTW}[i-1,j-1]);$$  
$$\quad\quad \text{if } i==0 \text{ and } j==0 \text{ then}$$  
$$\quad\quad\quad \text{DTW}[i,j] = \text{dist};$$  
$$\quad\quad \text{else}$$  
$$\quad\quad\quad \text{DTW}[i,j] = \text{minimum} + \text{dist};$$  
$$\quad \text{end}$$  
$$\text{end}$$  

**Algorithm 1:** Calculation of the distance matrix
A Dynamic Time Warping

**Input:** DTW
**Output:** WarpPath

vector<x,y> WarpPath;
i = N-1;
j = M-1;

**while** true **do**

<table>
<thead>
<tr>
<th>i==0 &amp;&amp; j==0 <strong>then</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td>break;</td>
</tr>
<tr>
<td><strong>if</strong> i==0 <strong>then</strong></td>
</tr>
<tr>
<td>j–;</td>
</tr>
<tr>
<td><strong>else</strong></td>
</tr>
<tr>
<td><strong>if</strong> j==0 <strong>then</strong></td>
</tr>
<tr>
<td>i–;</td>
</tr>
<tr>
<td><strong>else</strong></td>
</tr>
<tr>
<td>min = inf;</td>
</tr>
<tr>
<td><strong>if</strong> DTW[i-1][j]&lt;min <strong>then</strong></td>
</tr>
<tr>
<td>min = DTW[i-1][j];</td>
</tr>
<tr>
<td>i–;</td>
</tr>
<tr>
<td><strong>if</strong> DTW[i][j-1]&lt;min <strong>then</strong></td>
</tr>
<tr>
<td>min = matrix[i][j-1];</td>
</tr>
<tr>
<td>j–;</td>
</tr>
<tr>
<td><strong>if</strong> DTW[i-1][j-1]&lt;min <strong>then</strong></td>
</tr>
<tr>
<td>i–;</td>
</tr>
<tr>
<td>j–;</td>
</tr>
</tbody>
</table>

WarpPath.add(i,j);

**end**

**Algorithm 2:** Calculation of the warppath

**Input:** s,t,WarpPath
**Output:** s_dtw,t_dtw

for i = 0 to WarpPath.length **do**

| s_dtw[i] = s[WarpPath[i].x]; |
| t_dtw[i] = t[WarpPath[i].y]; |

**end**

**Algorithm 3:** Warping the trajectories