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Probing quasiparticle excitations in a hybrid single electron transistor

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We investigate the behavior of quasiparticles in a hybrid electron turnstile with the aim of improving its performance as a metrological current source. The device is used to directly probe the density of quasiparticles and monitor their relaxation into normal metal traps. We compare different trap geometries and reach quasiparticle densities below \(3 \mu m^{-3}\) for pumping frequencies of 20 MHz. Our data show that quasiparticles are excited both by the device operation itself and by the electromagnetic environment of the sample. Our observations can be modelled on a quantitative level with a sequential tunneling model and a simple diffusion equation. © 2012 American Institute of Physics. [http://dx.doi.org/10.1063/1.4730407]

Applications of superconductors generally rely on the fact that electronic excitations can be generated only if energy higher or equal to the gap energy \(\Delta\) is available. Hence the number of the excitations is ideally exponentially small at low temperatures and the properties specific for superconductors appear. If the number of excitations, typically characterized by the density of quasiparticles, increases, the superconducting features degrade. Such an effect has been studied in several devices such as superconducting qubits,1–4 superconductor-insulator-normal metal-insulator-superconductor (SINIS) microcooler,5–8 and kinetic inductance detectors.9,10 In this letter, we focus on the effects of quasiparticles on a hybrid single-electron turnstile. We use the Coulomb blockaded turnstile for direct and simple probing of the quasiparticle excitation density. The device operates as a charge pump and is a promising candidate for the realization of a metrological current source.11 We show experimentally that the quasiparticle excitations limit the current quantization. By optimizing the quasiparticle relaxation, however, we estimate that it is possible to reach metrological accuracy.

In order to observe how quasiparticles influence the performance of the turnstile, we designed samples (type A) where the quasiparticle relaxation in normal metal traps was purposefully delayed by extending the bare superconducting lines that connect the junctions to the traps. The beginning of this isolated superconducting line can be seen in the scanning electron microscope image of the turnstile in Fig. 1(a), where it connects to the normal metal island via oxide junctions that appear as lighter areas. Its extension is visible in (c) all the way through to the wide traps of overlapping superconductor and normal metal separated by an oxide layer. The sample shown in (b) (type B) has wide leads with normal metal traps close to the junctions to enable efficient quasiparticle evacuation. The samples were fabricated with the standard electron-beam lithography and shadow mask technique.12 We compare the behaviour of quasiparticles in SINIS turnstile samples with different geometries. The length of the isolated superconducting line (given by the separation of the transistor junction from the trap) was varied between \(l = 200 \text{ nm}\) and \(l = 20 \mu m\). Measurements were performed in a dilution refrigerator at a base temperature of approximately 60 mK.

Figure 1(d) shows the current-voltage characteristics of the turnstile sample presented in (a) and (c). The black line shows the current through the turnstile when the bias voltage \(V_b\) is swept across the superconducting gap and the gate potential \(V_g\) is varied between the gate open (\(n_g = 0.5\)) and the gate closed (\(n_g = 0\)) states. Simulations based on sequential tunneling are fitted to the data in order to extract the parameters of the superconducting gap \(\Delta = 216 \mu eV\), the charging energy of the island \(E_c = 0.74 \Delta\), and the tunnelling resistance of the junction \(R_T = 91 \Omega\), specific to each sample (see Table I for parameters of all samples measured). These simulations are shown in blue for the gate open and red for the gate closed state. On this coarse level, the heating

![Image](https://via.placeholder.com/150)

**FIG. 1.** (a) Scanning electron micrograph of the \(l = 20 \mu m\) type A SINIS20 turnstile showing the superconducting Al leads connected to the Cu metal island via AlO\(_2\) barrier junctions and the gate electrode used to regulate the potential of the island. (b) shows the type B SINIS20 geometry sample where the normal metal traps are within 200 nm of the junctions and the leads open up straight from the junction. In (c), the full length \(l\) of the superconducting line of sample SINIS20 between the junction and the trap is visible as well as the quasiparticle traps formed by overlapping Cu and Al shadows. A sketch of the basic measurement circuitry is depicted and (d) shows the IV characteristics of the turnstile.
of the superconducting leads does not make a significant contribution and can be neglected. The overheating of the normal metallic island (thickness 30 nm) is taken into account by considering the electron-phonon coupling with material parameter value of $\Sigma = 2 \times 10^9 \text{WK}^{-1}\text{m}^{-3}$ which is consistent with values obtained in previous experiments.\textsuperscript{13,14} In the subgap and pumping experiments, we have the opposite situation: the island does not heat since the signals are much smaller but as we look at small differences, the overheating of the superconductor starts to have an effect.

We now investigate the current of the turnstile more closely for bias voltages within the superconducting gap. These measurements allow the direct probing of the quasiparticle density. This is not possible with voltage biased NIS junctions that probe the excitations more indirectly\textsuperscript{5–8,15} and correspond to the gate open case in these experiments. Figure 2(a) shows the current as a function of $V_g$ for gate voltages varying between $-130.233.216.27$ On: Tue, 19 May 2015 06:09:48

<table>
<thead>
<tr>
<th>Sample</th>
<th>$E_c/\Delta$</th>
<th>$R_J$ (kΩ$_{1/2}$)</th>
<th>$l$ (µm)</th>
<th>$w_1$ (nm)</th>
<th>$w_2$ (µm)</th>
<th>$\sigma_I$ (Ωm$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SINIS20</td>
<td>0.74</td>
<td>91</td>
<td>21</td>
<td>120</td>
<td>5</td>
<td>$2.3 \times 10^6$</td>
</tr>
<tr>
<td>SINIS5</td>
<td>0.7</td>
<td>81</td>
<td>5.4</td>
<td>120</td>
<td>5</td>
<td>$2.7 \times 10^6$</td>
</tr>
<tr>
<td>SINIS1</td>
<td>0.7</td>
<td>85</td>
<td>1.1</td>
<td>160</td>
<td>5</td>
<td>$9.5 \times 10^6$</td>
</tr>
<tr>
<td>SINISopen</td>
<td>1.2</td>
<td>170</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$1.0 \times 10^6$</td>
</tr>
</tbody>
</table>

We measured the same sample in two different sample stages. Instead of having an enclosed stage with one metallic cover as in the measurement displayed in Fig. 2(a), we also used an indium sealed double hermetic metallic sample stage. In the latter case, the radio frequency (RF) line had an additional 20 cm thermocoax cable to enhance the sample shielding. This was not included in the wiring of the single cover stage. However, as the RF line is not electrically connected to the turnstile, we do not expect this to influence the direct heat conduction to the sample. The dc wiring of the two setups was similar made of approximately 2 m of thermocoax cable. The two sample stages are thermalized to the cryostat base temperature in an identical way and the sole purpose of this sealing is to create an RF shield to the sample. The result is shown in panel (b). In this case, no sub-gap current can be resolved. This behavior was fitted with temperatures of $T_S \leq 167 \text{ mK}$ and $T_N = 72 \text{ mK}$, which we present in Fig. 2(d). The inset in Fig. 2(d) displays the quasiparticle density $n_{qp}$ inferred from the relation $n_{qp} = 2D(E_F) \int_0^\infty n(E)e^{-E/k_BT}dE = \sqrt{2\pi} D(E_F)\sqrt{k_BT} / \Delta e^{-\Delta/k_BT}$ which is valid at low temperatures $k_BT \ll \Delta$ for three different samples with varying distance to the trap and measured with the poorly filtered sample stage. We use $D(E_F) = 1.45 \times 10^{47} \text{m}^{-3}\text{J}^{-1}$ as the normal state density of states at the Fermi energy.\textsuperscript{16} We observe a monotonous increase in $n_{qp}$ with increasing distance of the trap from the junction. We deduce that the presence of environmentally excited quasiparticles is determined by both the trap relaxation rate and the diffusion rate through the superconducting line.

Next, we turn to the dynamic case of the turnstile operation. In addition to environmental excitation, quasiparticles are now injected to the superconducting leads once in every pump cycle. The pumping frequency thus allows us to control the injected power and the number of quasiparticles. Figure 3 shows current plateaus measured on type A SINIS20 sample. Three bias voltages were chosen around the optimum operation voltage of $eV_b = \Delta$ (Ref. 17) ranging from $0.8\Delta/e$ to $1.6\Delta/e$. Two main effects were observed: a slight overshoot for the highest bias voltage at the beginning of the plateau and a spreading of the plateau value for different $V_g$.\textsuperscript{130.233.216.27 On: Tue, 19 May 2015 06:09:48

![Table I. Sample parameters.](image-url)
Simulations including single electron and two-electron Andreev processes were used to model the process. The peak of the current at the beginning of the plateaus can be reproduced by allowing for an Andreev current with a conduction channel area of 30 nm². This value is taken from previous experiments with similar samples. The spreading of the plateaus in Fig. 3 is caused by quasiparticle excitations and follows the expected behaviour with respect to variations in geometry and pumping operation as described below.

The spread increases with the pumping frequency from $\Delta f = 8 \text{fA}$ for 1 MHz (panel (a) of Fig. 3) to $\Delta f = 15 \text{fA}$ for 10 MHz (panel (b)). The injected power $P_\text{inj}$ increases with $f$ and we model this increase in mean number of quasiparticles in the superconductor by raising its temperature $T_S$. The bias-dependence of current on the plateau is not influenced by quasiparticle excitations and follows the expected function of $T$. The injected power is distributed evenly in all directions. We rewrite Eq. (1) in terms of quasiparticle density $n_{qp}$ by considering only the strong exponential dependencies on $T$ to obtain

$$\nabla^2 n_{qp} = \lambda^2 (n_{qp} - n_{qp0}),$$

where $\lambda = \sqrt{\frac{2a}{\sqrt{n_{qp0}(k_BT/)}}}^{1/2}$ and $n_{qp0}$ is the quasiparticle density of the superconductor when it is fully thermalised to the normal metal. Next, we solve Eq. (2) for three different sections of the bias line for type A samples. In the first part, we treat the bare aluminium line of length $l$ and constant width $w_1$ with no quasiparticle trapping ($P_\text{trap} = 0$). The next part deals with the widening of the lead from $w_1$ to $w_2$, where we also neglect quasiparticle trapping since its contribution in this section of the lead is small for our samples. Then, in the last part, the lead continues with a constant cross section of $w_2$ and is in contact with the quasiparticle trap: $P_\text{trap} \neq 0$. As a result, we obtain the quasiparticle density at the junction to be

$$n_{qp} = \frac{\sqrt{\pi}\epsilon^2 D(E_F)\rho_n P_{inj}}{\sqrt{2\Delta k_BT}wd} \left( l + \frac{w_1}{w_2} \log \left( \frac{w_1}{w_2} \right) + \frac{\lambda}{w_1} \frac{w_1}{w_2} \right).$$

The first term is the diffusion in the bare aluminium wire, the second term is the spreading to the wider line, and the last term arises from the relaxation to the trap. Similarly, we can solve the diffusion for the type B sample with opening bias lines. Here, we assume that the line starts at radius $r_0$ and the injected power is distributed evenly to all directions. We take $r_0 = 70 \text{nm}$ so that the area the power is injected into, $\frac{\pi r_0^2 d}{50 \text{nm}^2}$, matches the junction area of the sample. The quasiparticle density at the junction is then

$$n_{qp} = \frac{\sqrt{\pi}\epsilon^2 D(E_F)\rho_n P_{inj} K_0(r_0/\lambda)}{\sqrt{2\Delta k_BT} \theta r_0 d K_1(r_0/\lambda)},$$

where $K_n$ is the modified Bessel function of second kind and $\theta$ the opening angle of the line.

We now compare the quasiparticle relaxation in different sample geometries. From fits to measurements similar to those shown in Fig. 3, we extract $n_{qp}$ as a function of $f$. These values are displayed as dots in Fig. 4 for the SINIS20 (blue), the SINIS5 (green), and the SINISopen samples (red). Using the diffusion model described above, we calculate $n_{qp}$ as a function of $f$ corresponding to an injection power on the plateau given by $P_{inj} = ef\Delta$ (solid lines). The injected heat calculated from the simulations deviated less than 10% from this power even at the highest frequencies measured. We used $\rho_n = 31 \text{n\Omega m}$ as the normal state resistivity for all samples. Individual sample parameters used in the simulations are listed in Table I. The measured densities clearly show a linear behavior with increasing $f$ as predicted by the model (see Eqs. (3) and (4)). As indicated by the slopes for increasing length $l$ of the isolated line, the further the quasiparticle
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In the single electron transistor are those injected above the superconducting band gap during turnstile operation and the single electron transistor is, the slower the relaxation process is and the more trap lies from the oxide junction and the thinner the connecting line is, the slower the relaxation process is and the more the superconductor is heated. For the samples SINIS20 and SINIS5, a finite quasiparticle density is observed even in the absence of injected power. This density is of the same order of magnitude thicker and the trap ten times more transparent. Alternatively, the bias leads can be extended to the third dimension. The resistance of the junctions should be increased by a factor of four and charging energy to $E_c > 2\Delta$. Finally, the density of environmentally activated quasiparticles needs to be reduced to a level $n_{qp} \ll 0.1 \mu m^{-3}$ which has been demonstrated experimentally in a recent work. With these realistic modifications, we expect to reach metrological accuracy in turnstile operation.

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![Figure 4](https://example.com/figure4.png)

**Figure 4.** Quasiparticle density as a function of the driving gate voltage $f$. Fits to measurements including first and second order tunnelling processes are displayed as dots and quasiparticle densities derived from the diffusion model are displayed as solid lines. We compare two type A samples with delayed relaxation, SINIS20 (blue) and SINIS5 (green) and one type B sample SINISopen (red). Diagrams of the sample geometries are displayed in the upper part of the figure, dark colours representing quasiparticle traps, lighter areas the isolated superconducting lines, and the small black bulks the normal metal islands. Below, a diagram shows the two pathways to quasiparticle excitation, during pumping via the normal metal island and through interactions with the electromagnetic environment.